



The CS2411 is an online programmable, block-based architecture 1024-point FFT/IFFT core. It is based on a radix-4 / radix-16 algorithm that performs FFT/IFFT computation in four computation passes. This highly integrated application specific silicon core is available in both ASIC and FPGA versions that have been handcrafted by Amphion for maximum performance while minimizing power consumption and silicon area.





FEATURES

- On-line programmable FFT/IFFT core
- 13-bit complex input/output in two's complement format (26-bit complex word)
- 13-bit twiddle factors generated inside the core
- 16-bit fixed-point internal arithmetic operation
- Programmable shift down control
- Mixed radix-4 radix-16 architecture
- Transform performed in four computation passes with zero-waiting
- Simultaneous loading/downloading supported
- Both input and output in normal order
- No external memory required
- Optimized for both ASIC and FPGA technologies with the same functionality
- Fully synchronous design

KEY METRICS

- Logic Area: 34K gates
- Memory Area: 51K RAM
- Input Clock: 108 MHz

APPLICATIONS

- Communications modulation schemes
- Image processing
- Atmospheric imaging
- Spectral representation

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FAST FOURIER TRANSFORM

FFT (Fast Fourier Transform) and IFFT (Inverse Fast Fourier Transform) are algorithms computing 2^p-point discrete Fourier transform and inverse discrete Fourier transform, as defined below.

FFT:
$$Y(k) = \sum_{n=0}^{N-1} X(n) W_N^{-nk}$$
, k=0, 1, 3, ...N-1 [1]

IFFT:
$$Y(k) = \frac{1}{N} \sum_{n=0}^{N-1} X(n) W_N^{nk}$$
, k=0, 1, 3, ...N-+1 [2]

Where N=2^P and $e^{-j2\pi/N}$.

The computational complexity of FFT and IFFT is proportional to $Nlog_RN$, where R is the radix base on which FFT/IFFT is performed. The higher the radix, the less number of multiplication is required, however the more simultaneous multiple data access is required which causes the circuits to be more complicated. The radix-4 algorithm offers a balance between the computational and circuit complexity and is often used in construction of higher radix FFT computation units when designing high performance FFT/IFFT hardware.

CS2411 SYMBOL AND PIN DESCRIPTION

Table 1 describes input and output ports (shown graphically in Figure 2) of the CS2411 1024-point FFT/IFFT core. Unless otherwise stated, all signals are active high and bit(0) is the least significant bit.





Name	I/O	Width	Description
CLK	I	1	Clock signal, rising edge active
NotRST	I	1	Asynchronous global reset signal, active LOW
CLR	I	1	Clear (synchronous reset) and programming signal, active HIGH
IFFT	Ι	1	Programming signal specifying the transform type, loaded when CLR is active
SDC	I	3	Programming signal specifying the number of bits for the additional scaling down operation, loaded when CLR is active
XRe	I	13	Real component of input data X, in two's complement format
XIm	I	13	Imaginary component of input data X, in two's complement format
XBS	I	1	Input data X block start signal, active HIGH, associated with the first input data of the 1024-point block. The remaining data of the 1024-point data block is loaded into the core in the following clock cycles in the natural order.
YEnab	I	1	Output data Y enable control, active HIGH
STE*	I	1	Scan Test Enable Signal – ASIC version only During scan testing the memory block needs to be bypassed to allow the scan test to be performed. During test STE is set HIGH and the memory is bypassed. During normal operation STE is set LOW.
XBIP	0	1	Output signal indicating loading X is in Progress. XBIP goes to HIGH the next clock cycle when XBS is active and returns to LOW when the last data of the 1024-point block is loaded into the core. XBS is ignored when it is HIGH.
Busy	0	1	Output signal indicating the transform in progress (busy). It goes to HIGH the next clock cycle when the last data of the 1024-point block is loaded into the core and returns to LOW when the core is ready to accept the next input data block. XBS is ignored when it is HIGH.

Table 1: CS2411 - 1024 Point FFT / IFFT Interface Signal Definitions



Table 1: CS2411 - 1024 Point FFT / IFFT Interface Signal Definitions

Name	I/O	Width	Description
Done	0	1	Output signal indicating the transform result is available. It goes to HIGH when the core is ready to output transform result and returns to LOW when YEnab is asserted to download the result.
YBS	0	1	Output data Y block start signal, active HIGH, asserted when the first data of the 1024-point trans- formed block is available on the output port. The remaining data of the 1024-point transform result is available at the output of the core in the following clock cycles in natural order.
YAV	0	1	Output data Y available indicator, active HIGH, asserted with valid data of the 1024-point transform result
YRe	0	13	Real component of output data Y, in two's complement format, valid only when YAV is HIGH
Ylm	0	13	Imaginary component of output data Y, in two's complement format, valid only when YAV is HIGH
YOV	0	1	Output data Y overflow signal, active HIGH, asserted when overflow occurs when the transform is performed. It is reset when a new transform starts and is associated with the 1024-point block.

FUNCTIONAL DESCRIPTION

The CS2411 performs a mixed decimation in frequency (DIF), radix-4, forward or inverse Fast Fourier Transforms on a 1024point complex data block. The transform is scheduled in four computation passes. Data is loaded into the core in normal sequential (natural) order. The transform result comes out from the core in the natural order also. The core is on-line programmable on the transform type and scaling down control. The input and output data and the twiddle factor wordlengths have been chosen such that it can be used in a wide range of applications such as audio, video and communications.

The core computes the transform using fixed-point arithmetic with programmable shift down control on each computation passes to handle the possible wordlength growth and overflow in the transform. This achieves the maximal accuracy possible while maintaining the desired dynamic range for the output. The core is a synchronous design with all the flip-flops being triggered at the rising edge of the clock signal CLK.

PROGRAMMING THE CORE

Programming CS2411 is performed when the core is synchronously reset. This is done through asserting signal CLR and applying appropriate signals to the input ports IFFT and SDC. Port IFFT specifies the transform type i.e. FFT/IFFT Table 2 lists the FFT/IFFT value for programming the core to appropriate transform type.

Table 2: Programming Transform Type

Port IFFT	Transform Type
0	FFT
1	IFFT

The core performs 4-bit unconditional shifting down on the internal data during the 1024-point transform. However, theoretically the 1024-point FFT may have up to a total of 11-bits word growth. The CS2411 core can perform up to 4-bit unconditional shifting down and 7-bit controlled shifting down operation to avoid possible overflow and also to allow the transform gain to be controlled. This is programmed through port SDC. The total number of shift down bits decides the transform scaling down factor. Table 3 lists the SDC values for programming the scaling factor.

Table 3: Programming Scaling Factor

Port SDC	Fixed Shifting (Bits)	Additional Shifting (Bits)	Scaling Factor (2 ^{-(7+SDC)})
000	4	0	1/16
001	4	1	1/32
010	4	2	1/64
011	4	3	1/128
100	4	4	1/256
101	4	5	1/512
110	4	6	1/1024
111	4	7	1/2048

After the global asynchronous reset signal, RST is applied, the core is reset to the default mode: 1024-point FFT without the additional shifting operation. Programming the core can be performed at any time subsequently. The programming signals are valid only when CLR is asserted. This is illustrated in Figure 3. It is noted that when CLR is applied the core is reset as well.





INPUT AND OUTPUT DATA FORMAT

The input complex number data is represented by 13-bit real and imaginary components, namely XRe and XIm, in the two's complement format. The input data is loaded into the core in the normal order, i.e., X(0) enters the core first, followed by X(1) in the next clock cycle, and then X(2) in the following cycle, etc. In total it takes 1024 clock cycles for a data block to enter the core for FFT/IFFT processing.

The transform data is represented by complex numbers which consist of a 13-bit real component YRe and a 13-bit imaginary component YIm both in the two's complement format. The output data is burst out from the core when the transform has been performed to the stage that allows the result to be output and the output port is enabled. The result from the core is also in the normal order, i.e., Y(0) first, followed by Y(1), Y(2) and so on.

TRANSFORM COMPUTATION

The transform is scheduled to complete in four passes. In each pass the controller fetches the intermediate data from the internal dual port memory, sends it to the processing unit, fetches the computation results from the processing unit and writes the result back to memory for the next pass or for the output. The CS2411 employs a Cooley-Tukey radix-4 decimation-in-frequency (DIF) to compute the FFT/IFFT. This algorithm requires the calculation of radix-4 butterflies and twiddle multiplications in multiple passes. Theoretically the intermediate result value of a radix-4 butterfly with twiddle operation may grow by a factor of up to 5.657. This represents up to three-bit wordlength growth. In the last pass radix-16 operations are effectively performed. This will possibly result in additional one bit wordlength growth. The core performs one bit right-shift on the intermediate result unconditionally in the four passes. A rounding technique is employed to achieve the maximal computation accuracy possible. When the intermediate value is derived from the twiddle multiplication result, or the input to the butterfly is scaled down, round-to-the-nearest operation is performed. This gives the maximal computation accuracy possible for the given wordlength.

Table 4: Transform Operations in Each Pass

Transform Size	Pass 1	Pass 2	Pass 3	Pass 4
1024-point	Radix-4	Radix-4	Radix-4	Radix-16

The CS2411 core performs scaling down operation by right shifting the intermediate result in the four passes, according to the scaling down control programmed. Table 5 lists the relationship between the programming input signal SDC and the number of scaling down bits performed in the four passes. It is noted that there is no overflow in the computation when the total number of shifting bits is equal to 11 bits.

Table 5: Number of Right Shifting Bits in Each Pass

SDC	Pass 1	Pass 2	Pass 3	Pass 4	Total
000	1	1	1	1	4
001	2	1	1	1	5
010	2	2	1	1	6
011	2	2	1	1	7
100	3	2	2	1	8
101	3	2	2	2	9
110	3	2	2	3	10
111	3	2	2	4	11

FIXED WORD LENGTH AND ACCURACY

The CS2411 core uses fixed-point arithmetic to perform the transform. The twiddle factors (Sine and Cosine values), which are generated by the core internally, have 13-bit accuracy. At the end of each computation pass, the result is rounded to 13 bits. Figure 4 illustrates the word lengths at various computation stages in the CS2411 core.

The rounding technique is employed to achieve the maximal computation accuracy possible for the given word lengths. When the intermediate value is derived from the twiddle multiplication result, the output from the butterflies is scaled down, or the intermediate result is right shifted, the core performs the round-to-the-nearest operation to keep the loss of accuracy minimal.

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Table 6 gives the simulation results on the transform accuracy of CS2411 core. These results are obtained by applying 64 blocks of 13-bit random input data to the core and the scaling down control is set such that there is just no overflow in the computation. For example, the output magnitude is maximized while no overflow occurs. The 13-bit output data from the core is compared with the result of double precision FFT model. The error is measured in terms of the output LSB weight. It is noted that when overflow occurs the transform accuracy will be decreased severely.

Table 6: Simulation	n Results	of Transform	Accuracy
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Transform Size	1024-point
SDC setting	3
Scaling Factor	1/(2^7)
Number of complex data samples compared	64K
Maximal output Magnitude	2624
Maximal Error (Re)	7
Maximal Error (Imag)	7
Average Absolute Output	472.134
Average Absolute Error	0.851654
Mean Square Error	1.3474
Average SNR	54.876 dB



Figure 4: Word Length In Arithmetic Operations

LOADING INPUT AND DOWNLOADING RESULT

Loading the input data is performed under the control of XBS signal. The XBS signal should be asserted when the output signal XBIP and BUSY are LOW. It indicates the first data of the 1024-point data block. The data is clocked in on the clock rising edge. The remaining data of the 1024-point data block is loaded in on the rising edge of the clock in natural order successively.

When the core starts to load a 1024-point data block, signals XBIP and BUSY are asserted to indicate that loading of a data

block is in progress. Signal XBS will be ignored when XBIP is HIGH. When the last data of the block is loaded into the core, XBIP signal returns to LOW and signal BUSY stays HIGH to indicate the transform computation is in progress. Signal XBS is still ignored in this case until Busy returns to LOW.

The CS2411 core starts the transform prior to the completion of loading the 1024-point data block when the required data has been loaded, i.e., the input data loading is overlapped with the first computation pass. This compensates the latency introduced by the pipelined computation units so that the input data loading and the four computation passes can be completed in 5*1024 clock cycles. Signal Done goes to HIGH when the transform result is available (after 5093 cycles). Downloading of the transform result is started by asserting the input signal YEnab when Done is HIGH. Signal Done returns to LOW when downloading is started. The first sample of the transform result comes out from the core in the natural order two clock cycles later after YEnab is asserted. Output signal YAV is asserted when the data on port YRe and YIm are valid and output signal YBS is asserted when the first sample of the 1024-point result is on the output port. The output data burst out from the core in 1024 clock cycles. Downloading the result can be overlapped with the 4th computation pass to achieve 5*1024 clock cycles operation, if input signal YEnab is asserted as soon as the output signal Done goes to HIGH. The loading of the next data block can be started as soon as output signal Busy is de-asserted. Figure 5 shows the functional timing for the 5*1024 clock cycle I/O and transform operation. It is noted that the input signal YEnab can be constantly asserted and if so the transform result will be automatically downloaded when available.

It should be noted that the core waits for YEnab being asserted when signal Done goes HIGH to start the downloading process, allowing the user to control the transform data flow. The system clock rate is not restricted to the 5*1024 cycles and can be any rate higher than 5X the data rate. In this case if the downloading result has been completed but loading the next block is not started, signal Done will go to HIGH again to indicate that the transform result is still available in the internal memory and can be downloaded again. This feature can be utilized in C-OFDM modulation systems to perform the guard interval insertion. Figure 6 shows the operating flowchart for the CS2411 core.



Figure 5: 5*1024 Cycle I/O and Transform Timing



Figure 6: CS2411 Operating Flowchart



OVERFLOW HANDLING

CS2411 keeps track of the numeric values during the transform computation. If overflow occurs, due to the insufficient number of shifting down bits programmed for the given input data, the overflow value is saturated and the overflow flag signal (YOV) is asserted to alert the application system.

The overflow signal is flagged on-the-fly when the computation is in progress. It is automatically reset when a new transform is started.

PROCESSING TIME AND LATENCY

The processing time starts from when the last data of a data block is loaded into the core to when the transform has been completed and is a function of the transform size. It is equivalent to the time interval from when output signal Busy is asserted to when it is de-asserted and is measured in number of clock cycles listed. The real transform time depends on the clock frequency.

The transform period includes the transform time and the data I/O time. It indicates the number of clock cycles required for the core to perform one transform with input data loading and transform result downloading. The minimum transform period is obtained by asserting input signal YEnab as soon as the output signal Done is asserted and by starting the next data block as soon as output signal BUSY returns to LOW. Table 7 lists the transform time and minimum period for the transform size of 1024.

Table 7: CS2411 Processing Time and Transform Period

Transform Size	Processing Time (Clock cycles)	Minimum Transform Period (Clock cycles)
1024-point	4096	5120

AVAILABILITY AND IMPLEMENTATION INFORMATION

ASIC CORES

For applications that require the high performance, low cost and high integration of an ASIC, Amphion delivers application specific silicon cores that are pre-optimized to a targeted silicon technology by Amphion experts.

Consult your local Amphion representative for product specific performance information, current availability of individual products, and lead times on ASIC core porting.

Table 8: CS2411 ASIC Core

PRODUCT ID#	SILICON VENDOR	PROCESS	MAXIMUM FREQUENCY	LOGIC GATES	MEMORY AREA	AVAILABILITY
CS2411TK	TSMC	180 nm using Artisan standard Cell libraries	108 MHz	34K	51K Dual Port RAM	Now

PROGRAMMABLE LOGIC CORES

For ASIC prototyping or for projects requiring the fast time-to-market of a programmable logic solutions that offer the siliconaware performance tuning found in all Amphion products, combined with the rapid design times offered by today's leading programmable logic solutions.

PRODUCT ID	SILICON VENDOR	PROGRAMMABLE LOGIC PRODUCT	MAXIMUM FREQUENCY (MHz)	DEVICE RESOURCES USED (LOGIC)	DEVICE RESOURCES USED (MEMORY)	AVAILABILITY
CS2411XV*	Xilinx	Virtex-E	57	1639 Slices	9 BRAMs	Now

Table 9: Programmable Logic Cores

* The implementation information on ALTERA devices is available upon request.



ABOUT AMPHION

Amphion (formerly Integrated Silicon Systems) is the leading supplier of speech coding, video/ image processing and channel coding application specific silicon cores for system-on-a-chip (SoC) solutions in the broadband, wireless, and mulitmedia markets.

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