## Analog Multiplier

## Features

- High accuracy
- Nonlinearity - $0.1 \%$

Temperature coefficient $-0.005 \% /{ }^{\circ} \mathrm{C}$

- Multiple functions
- Multiply, divide, square, square root, RMS-to-DC
conversion, AGC and modulate/demodulate
- Wide bandwidth -4 MHz
- Signal-to-noise ratio - 94 dB


## Applications

- Low distortion audio modulation circuits
- Voltage-controlled active filters
- Precision oscillators


## Description

The RC4200 analog multiplier has complete compensation for nonlinearity, the primary source of error and distortion. This multiplier also has three onboard operational amplifiers designed specifically for use in multiplier logging circuits. These amplifiers are frequency compensated for optimum AC response in a logging circuit, the heart of a multiplier, and can therefore provide superior AC response.

The RC4200 can be used in a wide variety of applications without sacrificing accuracy. Four-quadrant multiplication, two-quadrant division, square rooting, squaring and RMS conversion can all be easily implemented with predictable accuracy. The nonlinearity compensation is not just trimmed at a single temperature, it is designed to provide compensation over the full temperature range. This nonlinearity compensation combined with the low gain and offset drift inherent in a well-designed monolithic chip provides a very high accuracy and a low temperature coefficient.

## Block Diagram



## Functional Description

The RC4200 multiplier is designed to multiply two input currents ( $\mathrm{I}_{1}$ and $\mathrm{I}_{2}$ ) and to divide by a third input current (I4). The output is also in the form of a current (I3). A simplified circuit diagram is shown in the Block Diagram. The nominal relationship between the three inputs and the output is:

$$
\begin{equation*}
I_{3}=\frac{I_{1} I_{2}}{I_{4}} \tag{1}
\end{equation*}
$$

The three input currents must be positive and restricted to a range of $1 \mu \mathrm{~A}$ to 1 mA . These currents go into the multiplier chip at op amp summing junctions which are nominally at zero volts. Therefore, an input voltage can be easily converted to an input current by a series resistor. Any number of currents may be summed at the inputs. Depending on the application, the output current can be converted to a voltage by an external op amp or used directly. This capabilty of combining input currents and voltages in various combinations provides great versatility in application.

Inside the multiplier chip, the three op amps make the collector currents of transistors Q1, Q2 and Q4 equal to their respective input currents ( $\mathrm{I}_{1}, \mathrm{I}_{2}$, and I 4 ). These op amps are designed with current source outputs and are phase-compensated for optimum frequency response as a multiplier. Power drain of the op amps was minimized to prevent the introduction of undesired thermal gradients on the chip. The three op amps operate on a single supply voltage (nominally -15 V ) and total quiescent current drain is less than 4 mA . These special op amps provide significantly improved performance in comparison to 741-type op amps.

The actual multiplication is done within the log-antilog configuration of the Q1-Q4 transistor array. These four transistors, with associated proprietary circuitry, were specially designed to precisely implement the relationship.

$$
\begin{equation*}
\mathrm{V}_{\mathrm{BEN}}=\frac{\mathrm{kT}}{\mathrm{Q}} \mathrm{In} \frac{\mathrm{I}_{\mathrm{CN}}}{\mathrm{I}_{\mathrm{SN}}} \tag{2}
\end{equation*}
$$

Previous multiplier designs have suffered from an additional undesired linear term in the above equation; the collector current times the emitter resistance. The ICrE term introduces a parabolic nonlinearity even with matched transistors. Fairchild Semiconductor has developed a unique and proprietary means of inherently compensating for this undesired ICrE term. Furthermore, this Fairchild Semiconductor developed circuit technique compensates linearity error over temperature changes. The nonlinearity versus temperature is significantly improved over earlier designs.

From equation (2) and by assuming equal transistor junction temperatures, summing base-to-emitter voltage drops around the transistor array yields:

$$
\begin{equation*}
\frac{\mathrm{KT}}{\mathrm{q}}\left[\operatorname{In} \frac{\mathrm{I}_{1}}{\mathrm{I}_{\mathrm{S} 1}}=\operatorname{In} \frac{\mathrm{I}_{2}}{\mathrm{I}_{\mathrm{S} 2}}-\operatorname{In} \frac{\mathrm{I}_{3}}{\mathrm{I}_{\mathrm{S} 3}}-\operatorname{In} \frac{\mathrm{I}_{4}}{\mathrm{I}_{\mathrm{S} 4}}\right]=0 \tag{3}
\end{equation*}
$$

This equation reduces to:
$\frac{\mathrm{I}_{1} \mathrm{I}_{2}}{\mathrm{I}_{3} \mathrm{I}_{4}}=\frac{\mathrm{I}_{\mathrm{S} 1} \mathrm{I}_{\mathrm{S} 2}}{\mathrm{I}_{\mathrm{S} 3} \mathrm{I}_{\mathrm{S} 4}}$
The rate of reverse saturation current IS1IS2/IS3IS4, depends on the transistor matching. In a monolithic multiplier this matching is easily achieved and the rate is very close to unity, typically $1.0 \pm 1 \%$. The final result is the desired relationship:

$$
\begin{equation*}
\mathrm{I}_{3}=\frac{\mathrm{I}_{1} \mathrm{I}_{2}}{\mathrm{I}_{4}} \tag{5}
\end{equation*}
$$

The inherent linearity and gain stability combined with low cost and versatility makes this new circuit ideal for a wide range of nonlinear functions.

## Pin Assignments



## Absolute Maximum Ratings

| Parameter |  | Min. | Max. | Unit |
| :--- | :--- | :---: | :---: | :---: |
| Supply Voltage $^{1}$ |  |  | -22 | V |
| Input Current |  |  | -5 | mA |
| Storage Temperature Range | RC4200/4200A | -55 | +125 | ${ }^{\circ} \mathrm{C}$ |
| Operating Temperature Range | RC4200/4200A | 0 | +70 | ${ }^{\circ} \mathrm{C}$ |

## Notes:

1. For a supply voltage greater than -22 V , the absolute maximum input voltage is equal to the supply voltage.
2. Observe package thermal characteristics.

## Thermal Characteristics

(Still air, soldered into PC board)

|  | 8-Lead Plastic DIP | 8-Lead SOIC |
| :--- | :---: | :---: |
| Maximum Junction Temperature | $+125^{\circ} \mathrm{C}$ | $+125^{\circ} \mathrm{C}$ |
| Maximum PD TA $50^{\circ} \mathrm{C}$ | 468 mW | 300 mW |
| Thermal Resistance $\theta \mathrm{JC}$ | - | - |
| Thermal Resistance $\theta \mathrm{JA}$ | $160^{\circ} \mathrm{C} / \mathrm{W}$ | $240^{\circ} \mathrm{C} / \mathrm{W}$ |
| For TA $>50^{\circ} \mathrm{C}$ Derate at | $6.25 \mathrm{~mW} /{ }^{\circ} \mathrm{C}$ | $4.17 \mathrm{~mW} /{ }^{\circ} \mathrm{C}$ |

## Electrical Characteristics

(Over operating temperature range, V s $=-15 \mathrm{~V}$ unless otherwise noted)

| Parameters | Test Conditlons | 4200A |  |  | 4200 |  |  | Units |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Min. | Typ. | Max. | Min. | Typ. | Max. |  |
| Total Error as Multiplier | TA $=+25^{\circ} \mathrm{C}$ |  |  |  |  |  |  |  |
|  | Untrimmed ${ }^{1}$ |  |  | $\pm 2.0$ |  |  | $\pm 3.0$ | \% |
|  | With External Trim |  | $\pm 0.2$ |  |  | $\pm 0.2$ |  | \% |
|  | Versus Temperature |  | $\pm 0.005$ |  |  | $\pm 0.005$ |  | \%/ ${ }^{\circ} \mathrm{C}$ |
|  | Versus Supply (-9 to -18V) |  | $\pm 0.1$ |  |  | $\pm 0.1$ |  | \%/V |
| Nonlinearity ${ }^{2}$ | $\begin{aligned} & 50 \mu \mathrm{~A} \leq \mathrm{I}_{1,2,4} \leq 250 \mu \mathrm{~A}, \\ & \mathrm{~T}_{\mathrm{A}}=+25^{\circ} \mathrm{C} \end{aligned}$ |  |  | $\pm 0.1$ |  |  | $\pm 0.3$ | \% |
| Input Current Range ( $\mathrm{I}_{1}, \mathrm{I}_{2}$ and I 4 ) |  | 1.0 |  | 1000 | 1.0 |  | 1000 | $\mu \mathrm{A}$ |
| Input Offset Voltage | $\begin{aligned} & \mathrm{I}_{1}=\mathrm{I}_{2}=\mathrm{I}_{4}=150 \mu \mathrm{~A} \\ & \mathrm{~T}_{\mathrm{A}}=+25^{\circ} \mathrm{C} \end{aligned}$ |  |  | $\pm 5.0$ |  |  | $\pm 10$ | mV |
| Input Bias Current | $\begin{aligned} & \mathrm{I}_{1}=\mathrm{I}_{2}=\mathrm{I}_{4}=150 \mu \mathrm{~A} \\ & \mathrm{~T}_{\mathrm{A}}=+25^{\circ} \mathrm{C} \end{aligned}$ |  |  | 300 |  |  | 500 | nA |
| Average Input Offset Voltage Drift | $\mathrm{I}_{1}=\mathrm{I}_{2}=\mathrm{I}_{4}=150 \mu \mathrm{~A}$ |  |  | $\pm 50$ |  |  | $\pm 100$ | $\mu \mathrm{V} /{ }^{\circ} \mathrm{C}$ |
| Output Current Range ( $\left.\mathrm{I}_{3}\right)^{3}$ |  | 1.0 |  | 1000 | 1.0 |  | 1000 | $\mu \mathrm{A}$ |

Electrical Characteristics (continued)
(Over operating temperature range, $\mathrm{V}_{\mathrm{S}}=-15 \mathrm{~V}$ unless otherwise noted)

| Parameters | Test Conditlons | 4200A |  |  | 4200 |  |  | Units |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Min. | Typ. | Max. | Min. | Typ. | Max. |  |
| Frequency Response, -3dB point Supply Voltage |  | -18 | $\begin{array}{r} 4.0 \\ -15 \end{array}$ | -9.0 | -18 | $\begin{array}{r} 4.0 \\ -15 \end{array}$ | -9.0 | $\begin{gathered} \mathrm{MHz} \\ \mathrm{~V} \end{gathered}$ |
| Supply Current | $\begin{aligned} & \mathrm{I}_{1}=\mathrm{I}_{2}=\mathrm{I}_{4}=150 \mu \mathrm{~A} \\ & \mathrm{~T}_{\mathrm{A}}=+25^{\circ} \mathrm{C} \end{aligned}$ |  |  | 4.0 |  |  | 4.0 | mA |

## Notes:

1. Refer to Figure 6 for example.
2. The input circuits tend to become unstable at $\mathrm{I}_{1}, \mathrm{I}_{2}, \mathrm{I}_{4}<50 \mu \mathrm{~A}$ and linearity decreases when $\mathrm{I}_{1}, \mathrm{I}_{2}, \mathrm{I}_{4}>250 \mu \mathrm{~A}$ (eq. @ $\mathrm{I}_{1}=\mathrm{I}_{2}=500 \mu \mathrm{~A}$, nonlinearity error $\approx 0.5 \%$ ).
3. These specifications apply with output ( $\mathrm{I}_{3}$ ) connected to an op amp summing junction. If desired, the output ( $\mathrm{I}_{3}$ ) at pin (4) can be used to drive a resistive load directly. The resistive load should be less than $700 \Omega$ and must be pulled up to a positive supply such that the voltage on pin (4) stays within a range of 0 to +5 V .

## Applications Discussion

## Current Multiplier/ Divider

The basic design criteria for all circuit configurations using the RC4200 multiplier is contained in equation (1), that is,

$$
\mathrm{I}_{3}=\frac{\mathrm{I}_{1} \mathrm{I}_{2}}{\mathrm{I}_{4}}
$$

The current-product-balance equation restates this as:

$$
\begin{equation*}
\mathrm{I}_{1} \mathrm{I}_{2}=\mathrm{I}_{3} \mathrm{I}_{4} \tag{6}
\end{equation*}
$$



Figure 1. Current Multiplier/Divider

## Dynamic Range and Stability

The precision dynamic range for the RC 4200 is from +50 $\mu \mathrm{A}$
to $+250 \mu \mathrm{~A}$ inputs for $\mathrm{I}_{1}, \mathrm{I}_{2}$ and $\mathrm{I}_{4}$. Stability and accuracy degrade if this range is exceeded.

To improve the stability for input currents less than $50 \mu \mathrm{~A}$, filter circuits (RSCS) are added to each input (see Figure 2).


Figure 2. Current Multiplier/Divider with Filters
Amplifier A1 is used to convert the I3 current to an output voltage.

Multiplier: $\mathrm{Vz}=$ constant $\neq 0$
Divider: $\mathrm{Vy}=$ constant $\neq 0$

## Voltage Multiplier/Divider



## Figure 3. Voltage Multiplier/Divider

Solving for $V_{0}=\frac{V_{X} V_{Y}}{V_{Z}} \frac{R_{0} R_{4}}{\mathrm{~V}_{1} R_{2}}$
For a multiplier circuit $\mathrm{V}_{\mathrm{Z}}=\mathrm{V}_{\mathrm{R}}=$ constant
Therefore: $\mathrm{V}_{0}=\mathrm{V}_{\mathrm{X}} \mathrm{V}_{\mathrm{Y}} \mathrm{K}$ where $\mathrm{K}=\frac{\mathrm{R}_{0} \mathrm{R}_{4}}{\mathrm{~V}_{\mathrm{R}} \mathrm{R}_{1} \mathrm{R}_{2}}$
For a divider circuit $\mathrm{V}_{\mathrm{Y}}=\mathrm{V}_{\mathrm{R}}=$ constant
Therefore: $\mathrm{V}_{0}=\frac{\mathrm{V}_{\mathrm{X}}}{\mathrm{V}_{\mathrm{Z}}} \mathrm{K}$ where $\mathrm{K}=\frac{\mathrm{V}_{\mathrm{R}} \mathrm{R}_{0} \mathrm{R}_{4}}{\mathrm{R}_{1} \mathrm{R}_{2}}$

## Extended Range

The input and output voltage ranges can be extended to include 0 and negative voltage signals by adding bias currents. The $\mathrm{R}_{S} C S$ filter circuits are eliminated when the input and biasing resistors are selected to limit the respective currents to $50 \mu \mathrm{~A}$ min. and $250 \mu \mathrm{~A}$ max.

## Extended Range Multiplier



Resistors $\mathrm{R}_{\mathrm{a}}$ and $\mathrm{R}_{\mathrm{b}}$ extend the range of the $\mathrm{V}_{\mathrm{X}}$ and $\mathrm{V}_{\mathrm{Y}}$ inputs by picking values such that:
$\mathrm{I}_{1}(\min )=.\frac{\mathrm{V}_{\mathrm{X}}(\text { min. })}{\mathrm{R}_{1}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{a}}}=50 \mu \mathrm{~A}$,
and $\mathrm{I}_{1}$ (max.) $=\frac{\mathrm{V}_{\mathrm{X}} \text { (max.) }}{\mathrm{R}_{1}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{a}}}=250 \mu \mathrm{~A}$,
also $\mathrm{I}_{2}($ min. $)=\frac{\mathrm{V}_{\mathrm{Y}}(\min .)}{\mathrm{R}_{2}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{b}}}=50 \mu \mathrm{~A}$,
and $\mathrm{I}_{2}($ max. $)=\frac{\mathrm{V}_{\mathrm{Y}}(\max .)}{\mathrm{R}_{2}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{b}}}=250 \mu \mathrm{~A}$.
Resistor RC supplies bias current for I3 which allows the output to go negative.

Resistors RCX and RCY permit equation (6) to balance, ie.:
$\left(\frac{\mathrm{V}_{\mathrm{X}}}{\mathrm{R}_{1}}+\frac{\mathrm{v}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{a}}}\right)\left(\frac{\mathrm{v}_{\mathrm{Y}}}{\mathrm{R}_{2}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{b}}}\right)=\left(\frac{\mathrm{v}_{0}}{\mathrm{R}_{0}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{C}}}+\frac{\mathrm{v}_{\mathrm{X}}}{\mathrm{R}_{\mathrm{CX}}}+\frac{\mathrm{v}_{\mathrm{Y}}}{\mathrm{R}_{\mathrm{CY}}}\right)\left(\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{D}}}\right)$
$\frac{\mathrm{V}_{\mathrm{Y}} \mathrm{V}_{\mathrm{X}}}{\mathrm{R}_{1} \mathrm{R}_{2}}+\frac{\mathrm{V}_{\mathrm{X}} \mathrm{V}_{\text {REF }}}{\mathrm{R}_{1} \mathrm{R}_{\mathrm{b}}}+\frac{\mathrm{V}_{\mathrm{Y}} \mathrm{V}_{\text {REF }}}{\mathrm{R}_{2} \mathrm{R}_{\mathrm{a}}}+\frac{\mathrm{V}_{\text {REF }}}{\mathrm{R}_{\mathrm{a}} \mathrm{R}_{\mathrm{b}}}=$
$\frac{v_{0} V_{\text {REF }}}{R_{0} R_{d}}+\frac{v_{X} V_{\text {REF }}}{R_{c x} R_{d}}+\frac{v_{Y} V_{\text {REF }}}{R_{C Y} R_{d}}+\frac{v_{\text {REF }}{ }^{2}}{R_{c} R_{d}}$

## Cross-Product Cancellation

Cross-products are a result of ths $\mathrm{V}_{X} \mathrm{~V}_{\mathrm{R}}$ and $\mathrm{V}_{\mathrm{Y}} \mathrm{V}_{\mathrm{R}}$ terms.
To the extend that $R_{1} R_{b}=R_{C X} R_{D}$, and $R_{2} R_{a}=R_{C Y} R_{d}$ cross-product cancellation will occur.

## Arithmetic Offset Cancellation

The offset caused by the $V_{\text {REF }}{ }^{2}$ term will cancel to the extent that $\mathrm{R}_{\mathrm{a}} \mathrm{R}_{\mathrm{b}}=\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}$, and the result is:
$\frac{\mathrm{V}_{\mathrm{Y}} \mathrm{V}_{\mathrm{X}}}{\mathrm{R}_{1} \mathrm{R}_{2}}=\frac{\mathrm{V}_{0} \mathrm{~V}_{\text {REF }}}{\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}}$ or $\mathrm{V}_{0}=\mathrm{V}_{\mathrm{X}} \mathrm{V}_{\mathrm{Y}} \mathrm{K}$
where $\mathrm{K}=\frac{\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}}{\mathrm{V}_{\mathrm{REF}} \mathrm{R}_{1} \mathrm{R}_{2}}$

## Resistor Values

Inputs:
$\mathrm{V}_{\mathrm{X}}($ min. $) \leq \mathrm{V}_{\mathrm{X}} \leq \mathrm{V}_{\mathrm{X}}($ max. $)$
$\Delta \mathrm{V}_{\mathrm{X}}=\mathrm{V}_{\mathrm{X}}($ max. $)-\mathrm{V}_{\mathrm{X}}($ min. $)$
$\mathrm{V}_{\mathrm{Y}}($ min. $) \leq \mathrm{V}_{\mathrm{Y}} \leq \mathrm{V}_{\mathrm{Y}}($ max. $)$
$\Delta \mathrm{V}_{\mathrm{Y}}=\mathrm{V}_{\mathrm{Y}}($ max. $)=\mathrm{V}_{\mathrm{Y}}($ min. $)$
$\mathrm{V}_{\mathrm{REF}}=$ Constant $(+7 \mathrm{~V}$ to $+18 \mathrm{~V})$
$\mathrm{K}=\frac{\mathrm{V}_{0}}{\mathrm{~V}_{\mathrm{X}} \mathrm{V}_{\mathrm{Y}}}$ (Design Requirements)

Figure 4. Extended Range Multiplier
$\mathrm{R}_{1}=\frac{\Delta \mathrm{V}_{\mathrm{X}}}{200 \mu \mathrm{~A}}, \mathrm{R}_{2}=\frac{\Delta \mathrm{V}_{\mathrm{Y}}}{200 \mu \mathrm{~A}}, \mathrm{R}_{\mathrm{d}}=\frac{\mathrm{V}_{\mathrm{REF}}}{250 \mu \mathrm{~A}}$
$\mathrm{R}_{\mathrm{a}}=\frac{\Delta \mathrm{V}_{\mathrm{X}} \mathrm{V}_{\text {REF }}}{\left.250 \mu \mathrm{~A} \Delta \mathrm{~V}_{\mathrm{X}}-200 \mu \mathrm{~A} \mathrm{~V}_{\mathrm{X}} \text { (max. }\right)}$

$\mathrm{R}_{\mathrm{c}}=\frac{\mathrm{R}_{\mathrm{a}} \mathrm{R}_{\mathrm{b}}}{\mathrm{R}_{\mathrm{d}}}, \mathrm{R}_{\mathrm{CX}}=\frac{\mathrm{R}_{1} \mathrm{R}_{\mathrm{b}}}{\mathrm{R}_{\mathrm{d}}}, \mathrm{R}_{\mathrm{cy}}=\frac{\mathrm{R}_{2} \mathrm{R}_{\mathrm{a}}}{\mathrm{R}_{\mathrm{d}}}$
$\mathrm{R}_{0}=\frac{\Delta \mathrm{V}_{\mathrm{X}} \Delta \mathrm{V}_{\mathrm{Y}} \mathrm{K}}{160 \mu \mathrm{~A}}$

## Multiplying Circuit Offset Adjust

$10 \mathrm{~K} \leq \mathrm{R}_{5}=\mathrm{R} 9=\mathrm{R} 16 \leq 50 \mathrm{~K}$
$\mathrm{R}_{7}=\mathrm{R}_{11}=\mathrm{R}_{14},=100 \Omega$
$\mathrm{R}_{6}=\mathrm{R}_{10}=100 \Omega(\mathrm{VS} / 0.05)$
$\mathrm{R}_{15}=100 \Omega(\mathrm{VS} / 0.10)$
$\mathrm{R}_{8}=\mathrm{R}_{1} \| \mathrm{R}_{\mathrm{a}}$
$\mathrm{R}_{12}=\mathrm{R}_{2} \| \mathrm{Rb}_{\mathrm{b}}$
$R_{13}=R_{0}\left\|R_{C}\right\| R_{C X} \| R_{C Y}$


Figure 5. Multiplying Circuit Offset Adjust

## Procedure

1. Set all trimmer pots to 0 V on the wiper.
2. Connect $\mathrm{V}_{\mathrm{X}}$ input to ground. Put in a full scale square wave on $V_{Y}$ input. Adjust $\operatorname{XOS}(\mathrm{R} 5)$ for no square wave on $\mathrm{V}_{0}$ output (adjust for 0 feedthrough).
3. Connect $V_{Y}$ input to ground. Put in a full scale square wave on $V_{X}$ input. Adjust $\operatorname{YOS}(\mathrm{R} 9)$ for no square wave on $V_{0}$ output (adjust for 0 feedthrough).
4. Connect $\mathrm{V}_{\mathrm{X}}$ and VY to ground. Adjust $\operatorname{VOS}(\mathrm{R} 16)$ for 0 V on $\mathrm{V}_{0}$ output.

## Extended Range Divider



Figure 6. Extended Range Divider
As with the extended range multiplier, resistors $\mathrm{R}_{\mathrm{az}}$ and $\mathrm{R}_{\mathrm{ao}}$ are added to cancel the cross-product error caused by the biasing resistors, i.e.
$\left(\frac{\mathrm{V}_{\mathrm{X}}}{\mathrm{R}_{1}}+\frac{\mathrm{V}_{0}}{\mathrm{R}_{\mathrm{ao}}}+\frac{\mathrm{V}_{\mathrm{Z}}}{\mathrm{R}_{\mathrm{az}}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{a}}}\right)\left(\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{b}}}\right)=\left(\frac{\mathrm{V}_{0}}{\mathrm{R}_{0}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{C}}}\right)\left(\frac{\mathrm{V}_{\mathrm{Z}}}{\mathrm{R}_{4}}+\frac{\mathrm{V}_{\mathrm{REF}}}{\mathrm{R}_{\mathrm{D}}}\right)$
$\frac{v_{X} V_{\text {REF }}}{R_{1} R_{b}}+\frac{v_{0} V_{\text {REF }}}{R_{a 0} R_{b}}+\frac{v_{Z} V_{\text {REF }}}{R_{a z} R_{b}}+\frac{v_{\text {REF }}}{R_{a} R_{b}}=$
$\frac{\mathrm{v}_{0} \mathrm{v}_{\mathrm{Z}}}{\mathrm{R}_{0} \mathrm{R}_{4}}+\frac{\mathrm{v}_{0} \mathrm{~V}_{\text {REF }}}{\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}}+\frac{\mathrm{v}_{\mathrm{Z}} \mathrm{V}_{\text {REF }}}{\mathrm{R}_{4} \mathrm{R}_{\mathrm{c}}}+\frac{\mathrm{V}_{\text {REF }}{ }^{2}}{\mathrm{R}_{\mathrm{c}} \mathrm{R}_{\mathrm{d}}}$
To cancel cross-product and arithmetic offset:
$\mathrm{R}_{\mathrm{ao}} \mathrm{R}_{\mathrm{b}}=\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}, \mathrm{R}_{\mathrm{az}} \mathrm{R}_{\mathrm{b}}=\mathrm{R}_{4} \mathrm{R}_{\mathrm{c}}$ and $\mathrm{R}_{\mathrm{a}} \mathrm{R}_{\mathrm{b}}=\mathrm{R}_{\mathrm{c}} \mathrm{R}_{\mathrm{d}}$
and the result is:
$\frac{\mathrm{V}_{\mathrm{X}} \mathrm{V}_{\text {REF }}}{\mathrm{R}_{1} \mathrm{R}_{\mathrm{b}}}=\frac{\mathrm{V}_{0} \mathrm{~V}_{\mathrm{Z}}}{\mathrm{R}_{0} \mathrm{R}_{4}}$ or $\quad \mathrm{V}_{0}=\frac{\mathrm{V}_{\mathrm{X}}}{\mathrm{V}_{\mathrm{Z}} \mathrm{K}}$
where $\mathrm{K}=\frac{\mathrm{V}_{\mathrm{REF}} \mathrm{R}_{0} \mathrm{R}_{4}}{\mathrm{R}_{1} \mathrm{R}_{\mathrm{b}}}$

Notice that it is necessary to match the above resistor crossproducts to within the amount of error tolerable in the output offset, i.e., with a 10 V F.S. output, $0.1 \%$ resistor crossproduct match will give $0.1 \% \times 10 \mathrm{~V}$. untrimmable output offset voltage.

## Resistor Values

## Inputs:

$\mathrm{VX}(\min .) \leq \mathrm{VX}_{\mathrm{X}} \leq \mathrm{VX}$ (max.)
$\Delta \mathrm{V}_{\mathrm{X}}=\mathrm{V}_{\mathrm{X}}($ max. $)=\mathrm{V}_{\mathrm{X}}($ min. $)$
VZ (min.) $\leq \mathrm{V}_{\mathrm{Z}} \leq \mathrm{V}_{\mathrm{Z}}(\max$.
$\Delta \mathrm{V}_{\mathrm{Z}}=\mathrm{V}_{\mathrm{Z}}($ max. $)=\mathrm{V}_{\mathrm{Z}}(\min$.
VREF $=$ Constant $(+7 \mathrm{~V}$ to $+18 \mathrm{~V})$

## Outputs:

$\mathrm{V}_{0}$ (min.) $\leq \mathrm{V}_{0} \leq \mathrm{V}_{0}$ (max.)
$\Delta \mathrm{V}_{0}=\mathrm{V}_{0}$ (max.) $=\mathrm{V}_{0}$ (min.)
$\mathrm{K}=\frac{\mathrm{V}_{0} \mathrm{~V}_{\mathrm{Z}}}{\mathrm{V}_{\mathrm{X}}}$ (Design Requirement)
$\mathrm{R}_{0}=\frac{\Delta \mathrm{V}_{0}}{750 \mu \mathrm{~A}}, \mathrm{R}_{\mathrm{b}}=\frac{\Delta \mathrm{V}_{\mathrm{REF}}}{250 \mu \mathrm{~A}}, \mathrm{R}_{4}=\frac{\Delta \mathrm{V}_{\mathrm{Z}}}{200 \mu \mathrm{~A}}$
$\mathrm{R}_{\mathrm{c}}=\frac{\Delta \mathrm{V}_{0} \mathrm{~V}_{\text {REF }}}{750 \mu \mathrm{~A} \Delta \mathrm{~V}_{0}-700 \mu \mathrm{~A} \mathrm{~V}_{0}(\text { max. })}$
$\mathrm{R}_{\mathrm{d}}=\frac{\Delta \mathrm{V}_{\mathrm{X}} \mathrm{V}_{\mathrm{REF}}}{250 \mu \mathrm{~A} \Delta \mathrm{~V}_{\mathrm{Z}}-200 \mu \mathrm{~A} \mathrm{~V}} \mathrm{~V}_{\mathrm{Z}}$ (max.) $)$
$\mathrm{R}_{\mathrm{a}}=\frac{\mathrm{R}_{\mathrm{c}} \mathrm{R}_{\mathrm{d}}}{\mathrm{R}_{\mathrm{b}}}, \mathrm{R}_{\mathrm{az}}=\frac{\mathrm{R}_{\mathrm{c}} \mathrm{R}_{4}}{\mathrm{R}_{\mathrm{b}}}, \mathrm{R}_{\mathrm{ao}}=\frac{\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}}{\mathrm{R}_{\mathrm{b}}}$
$R_{1}=\frac{\Delta V_{0} \Delta V_{Z}}{600 \mu A K}$

## Divider Circuit with Offset Adjustment



## General

$10 \mathrm{~K} \leq \mathrm{R}_{5}=\mathrm{R}_{13}=\mathrm{R}_{17} \leq 50 \mathrm{~K}$
$R_{7}+R_{8} \approx R_{1}| | R_{a}| | R_{a z}| | R_{a o}$
$\mathrm{R}_{6} \approx \mathrm{R}_{7}$ (Vs/0.05)
$\mathrm{R} 9=\mathrm{Rb}$
$R_{10} \approx 100 \times R_{4}$
$\mathrm{R}_{11}=20 \mathrm{~K}$
$\mathrm{R}_{12}=100 \mathrm{~K}$
$R_{14}+R_{15} \approx R_{0} \| R_{c}$
$\mathrm{R}_{16} \approx \mathrm{R}_{15}$ (Vs/0.10)

Example: Two-Quad Divider
$V_{0}=K(V x / V Z), K=k, V_{R E F}=+V S=+15 V$
$-10 \leq \mathrm{V} \mathrm{X} \leq+10$, therefore $\Delta \mathrm{V} \mathrm{X}=20$
$0 \leq \mathrm{V} Z \leq+10$, therefore $\Delta \mathrm{V} Z=20$
$-10 \leq \mathrm{V}_{0} \leq+10$, therefore $\Delta \mathrm{V}_{0}=20$

| $R_{0}=26.7 \mathrm{~K}$ | $R_{1}=333 \mathrm{~K}$ |
| :--- | :--- |
| $R_{b}=60 \mathrm{~K}$ | $R_{5}, R_{13}, R_{17}=10 \mathrm{~K}$ |
| $R_{4}=50 \mathrm{~K}$ | $R_{7}, R_{15}=1 \mathrm{~K}$ |
| $R_{c}=37.5 \mathrm{~K}$ | $R_{8}, R_{11}=20 \mathrm{~K}$ |
| $R_{d}=300 \mathrm{~K}$ | $R_{6}, R_{9}, R_{16}=300 \mathrm{~K}$ |
| $R_{a}=187.5 \mathrm{~K}$ | $R_{10}=4.7 \mathrm{M}$ |
| $R_{a z}=31.25$ | $R_{12}=100 \mathrm{~K}$ |
| $R_{a 0}=133 \mathrm{~K}$ |  |

$R b=60 K$
$\mathrm{R}_{5}, \mathrm{R}_{13}, \mathrm{R}_{17}=10 \mathrm{~K}$
$R_{7}, R_{15}=1 \mathrm{~K}$
$\mathrm{R}_{8}, \mathrm{R}_{11}=20 \mathrm{~K}$
R6, R9, R16 $=300 \mathrm{~K}$
R10 $=4.7 \mathrm{M}$
$\mathrm{R}_{12}=100 \mathrm{~K}$

## Divider Circuit Offset Adjustment Procedure

1. Set each trimmer pot to 0 V on the wiper.
2. Connect $\mathrm{V}_{\mathrm{X}}$ (input) to ground. Put a DC voltage of approximatey $1 / 2 \mathrm{VZ}$ (max.) DC on the VZ (input) with an AC (squarewave is easiest) voltage of $1 / 2 \mathrm{VZ}$ (max.) peak-to-peak superimposed on it. Adjust XOS (R5) for zero feedthrough. (No AC at $\mathrm{V}_{0}$ )

3. Connect $\mathrm{VX}_{\mathrm{X}}$ (input) to VZ (input) and put in the $1 / 2 \mathrm{VZ}$ (max.) DC with an AC of approximately 20 mV less than VZ (max.).

Adjust ZOS (R13) for zero feedthrough.

4. Return $\mathrm{V}_{\mathrm{X}}$ (Input) to ground and connect VZ (max.) DC on $\mathrm{V}_{\mathrm{Z}}$ (input). Adjust output $\operatorname{VOS}\left(\mathrm{R}_{17}\right)$ for $\mathrm{V}_{\mathrm{O}}=$ 0 Vo
5. Connect $\mathrm{V}_{\mathrm{X}}$ (input) to $\mathrm{V}_{\mathrm{Z}}$ (input) and and in $\mathrm{V}_{\mathrm{Z}}$ (max.) DC. (The output will equal K.) Decrease the input slowly until the output $\left(\mathrm{V}_{0}-\mathrm{K}\right)$ deviates beyond the desired accuracy. Adjust ZOS to bring it back into tolerance and return to Step 4. Continue steps 4 and 5 until VZ reduces to the lowest value desired.

Notice that as the input to VX and VZ gets closer to zero (an illegal state) the system noise will predominate so much that an integrating voltmeter will be very helpful.

## Square Root Circuit $\mathbf{V o}_{0}=\mathbf{N} \sqrt{ } \mathbf{V} \mathbf{X}$



Figure 8.
$\frac{v_{X} V_{\text {REF }}}{R_{1} R_{b}}+\frac{v_{\text {REF }}}{R_{a} R_{b}}+\frac{v_{0} V_{\text {REF }}}{R_{a 0} R_{b}}=\frac{v_{0}^{2}}{R_{0} R_{4}}+\frac{v_{0} v_{\text {REF }}}{R_{c} R_{4}}+\frac{v_{0} V_{\text {REF }}}{R_{0} R_{d}}+\frac{v_{\text {REF }}{ }^{2}}{R_{c} R_{d}}$
If $R_{a} R_{b}=R_{c} R_{d}$ and $R_{a o} R_{b} R_{0} R_{d}+R_{a o} R_{b} R_{c} R_{4}=R_{c} R_{d} R_{0} R_{4}$

and $\mathrm{V}_{0}=\mathrm{N} \sqrt{\mathrm{V}_{\mathrm{X}}}$ where $\mathrm{N}=\sqrt{\mathrm{K}}$
$0 \leq \mathrm{V}_{\mathrm{X}} \leq \mathrm{V}_{\mathrm{X}}$ (max.) and $\mathrm{V}_{0}(\max )=.\mathrm{N} \sqrt{\mathrm{V}_{\mathrm{X}}{ }^{(\max .)}}$
$\mathrm{N}=\frac{\mathrm{V}_{0}}{\sqrt{\mathrm{~V}_{\mathrm{X}}}}$ (Design Requirements)
$\mathrm{R}_{1}=\frac{\mathrm{V}_{0}(\text { max. })^{2}}{74 \mu \mathrm{~A} \mathrm{~N}}$
$\mathrm{R}_{\mathrm{a}}=\mathrm{R}_{\mathrm{d}}=\frac{\mathrm{V}_{\text {REF }}}{50 \mu \mathrm{~A}}$
$\mathrm{R}_{\mathrm{b}}=\mathrm{R}_{\mathrm{c}}=\frac{\mathrm{V}_{\mathrm{REF}}}{150 \mu \mathrm{~A}}$
$\mathrm{R}_{4}=\frac{\mathrm{V}_{0}(\text { max. })}{50 \mu \mathrm{~A}}$
$\mathrm{R}_{\mathrm{ao}}=\frac{\mathrm{V}_{0}(\text { max. })}{125 \mu \mathrm{~A}}$
$R_{0}=\frac{V_{0} \text { (max.) }}{225 \mu \mathrm{~A}}$

## Square Root Circuit Offset Adjust



Figure 9. Square Root Circuit Offset Adjust
$10 \mathrm{~K} \leq \mathrm{R}_{5}=\mathrm{R}_{13} \leq 50 \mathrm{~K}$
$\mathrm{R}_{7}=100 \Omega$
$\mathrm{R}_{6}=\mathrm{R}_{7} \frac{\mathrm{~V}_{\mathrm{S}}}{0.05}$
$\mathrm{R}_{8}=\mathrm{R}_{1}\left\|\mathrm{R}_{\mathrm{a}}\right\| \mathrm{R}_{\mathrm{ao}}$
$\mathrm{R}_{9}=\mathrm{R}_{\mathrm{b}}$
$\mathrm{R}_{10}=\mathrm{R}_{0} \| \mathrm{R}_{\mathrm{C}}$
$\mathrm{R}_{11}=100 \Omega$
$\mathrm{R}_{12}=\mathrm{R}_{11} \frac{\mathrm{~V}_{\mathrm{S}}}{0.1}$

## Procedure

1. Set both trimmer pots to 0 V on the wiper.
2. Put in a full scale ( 0 to $V_{X}$ (max.) squarewave on $V_{X}$ input. Adjust $\operatorname{XOS}(\mathrm{R} 5)$ for proper peak-to-peak amplitude on $V_{0}$ output. (Scaling adjust)
3. Connect VX input to ground. $\operatorname{Adjust} \operatorname{VOS}(\mathrm{R} 13)$ for 0 V on $\mathrm{V}_{0}$ output.

## Squaring Circuits $\mathrm{V}_{0}=\mathrm{K} \mathrm{Vx}^{2}$



Figure 10. Squaring Circuit
$\frac{\mathrm{V}_{\mathrm{X}}^{2}}{\mathrm{R}_{1}{ }^{2}}+\frac{2 \mathrm{~V}_{\mathrm{X}} \mathrm{V}_{\text {REF }}}{\mathrm{R}_{1} \mathrm{R}_{\mathrm{a}}}+\frac{\mathrm{V}_{\text {REF }}{ }^{2}}{\mathrm{R}_{\mathrm{a}}{ }^{2}}=\frac{\mathrm{V}_{0} \mathrm{~V}_{\text {REF }}}{\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}}+\frac{\mathrm{V}_{\mathrm{REF}}{ }^{2}}{\mathrm{R}_{\mathrm{c}} \mathrm{R}_{\mathrm{d}}}+\frac{\mathrm{V}_{\mathrm{X}} \mathrm{V}_{\text {REF }}}{\mathrm{R}_{\mathrm{c}} \mathrm{R}_{\mathrm{d}}}$
if $\mathrm{R}_{\mathrm{a}}^{2}=\mathrm{R}_{\mathrm{c}} \mathrm{R}_{\mathrm{d}}$ and $\mathrm{R}_{1} \mathrm{R}_{\mathrm{a}}=2 \mathrm{R}_{\mathrm{CX}} \mathrm{R}_{\mathrm{D}}$
then $\frac{\mathrm{V}_{0} \mathrm{~V}_{\text {REF }}}{\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}}=\frac{\mathrm{V}_{\mathrm{X}}{ }^{2}}{\mathrm{R}_{1}{ }^{2}}$ or $\mathrm{V}_{0}=\mathrm{KV}_{\mathrm{X}}{ }^{2}$ where $\mathrm{K}=\frac{\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}}{\mathrm{V}_{\mathrm{REF} \mathrm{R}_{1}{ }^{2}}{ }^{2}}$
$\mathrm{V}_{\mathrm{X}}(\min .) \leq \mathrm{V}_{\mathrm{X}} \leq \mathrm{V}_{\mathrm{X}}(\max .) \quad \Delta \mathrm{V}_{\mathrm{X}}=\mathrm{V}_{\mathrm{X}}(\max )-.\mathrm{V}_{\mathrm{X}}(\min$.
$\mathrm{K}=\frac{\mathrm{V}_{0}}{\mathrm{~V}_{\mathrm{X}}{ }^{2}}$ (Design Requirement)
$R_{1}=\frac{\Delta V_{X}}{200 \mu \mathrm{~A}}$
$\mathrm{R}_{\mathrm{a}}=\frac{\Delta \mathrm{V}_{\mathrm{X}} \mathrm{V}_{\text {REF }}}{250 \mu \mathrm{~A} \Delta \mathrm{~V}_{\mathrm{X}}-200 \mu \mathrm{~A} \mathrm{~V}_{\mathrm{X}}(\text { max. })}$
$R_{d}=\frac{V_{R E F}}{250 \mu \mathrm{~A}}$
$\mathrm{R}_{\mathrm{c}}=\frac{\mathrm{R}_{\mathrm{a}}{ }^{2}}{\mathrm{R}_{\mathrm{d}}}$
$\mathrm{R}_{\mathrm{cx}}=\frac{\mathrm{R}_{1} \mathrm{R}_{\mathrm{a}}}{2 \mathrm{R}_{\mathrm{d}}}$
$\mathrm{R}_{0}=\frac{\Delta \mathrm{V}_{\mathrm{X}}{ }^{2} \mathrm{~K}}{160 \mu \mathrm{~A}}$

## Squaring Circuits Offset Adjust



Figure 11. Squaring Circuit Offset Adjust
$10 \mathrm{~K} \leq \mathrm{R}_{10}=\mathrm{R}_{11} \leq 50 \mathrm{~K}$
$\mathrm{R}_{8}, \mathrm{R}_{15}=100 \Omega$
$R_{9}, R_{14}=100 \Omega \frac{V_{S}}{0.1}$
$\mathrm{R}_{5}, \mathrm{R}_{6}=\mathrm{R}_{1} \| \mathrm{R}_{\mathrm{a}}$
$\mathrm{R}_{16}=\mathrm{R}_{0}\left\|\mathrm{R}_{\mathrm{c}}\right\| \mathrm{R}_{\mathrm{a}}$

## Procedure

1. Set both trimmer pots to 0 V on the wiper.
2. Put in a full scale $\left( \pm \mathrm{V}_{\mathrm{X}}\right)$ squarewave on $\mathrm{V}_{\mathrm{X}}$ input. Adjust ZOS(R10) for uniform output.
3. Connect $\mathrm{V}_{\mathrm{X}}$ input to ground. Adjust $\operatorname{VOS}\left(\mathrm{R}_{11}\right)$ for 0 V on $V_{0}$ outputs.

## Appendix 1-System Errors

There are four types of accuracy errors which affect overall system performance. They are:

- Nonimearity-Incremental deviation from absolute accuracy. See Note 1.
- Scaling Error-Linear deviation from absolute accuracy.
- Output Offset-Constant deviation from absolute accuracy.
- Feedthrough.-Cross-product errors caused by input offsets and external circuit limitations. See Note 2.

This nonlinearity error in the transfer function of the RC4200 is $\pm 0.1 \%$ maximum ( $\pm 0.03$ maximum for the RC4200A). That is,

$$
\mathrm{I}_{3}=\frac{\mathrm{I}_{1} \mathrm{I}_{2}}{\mathrm{I}_{4}} \pm 0.1 \% \text { F.S. }{ }^{(4)}
$$

The other system errors are caused by voltage offsets on the inputs of the RC4200 and can be as high as $\pm 3.0 \%( \pm 2.0 \%$ for RC4200A).

$$
\mathrm{V}_{0}=\frac{\mathrm{V}_{\mathrm{X}} \mathrm{~V}_{\mathrm{Y}}}{\mathrm{~V}_{\mathrm{Z}}} \frac{\mathrm{R}_{0} \mathrm{R}_{4}}{\mathrm{R}_{1} \mathrm{R}_{2}} \pm 3.0 \% \text { F.S. }{ }^{(3)(4)}
$$



65-1871
Figure 12.

## Notes:

1. The input circuits tend to become unstable at
$\mathrm{I}_{1}, \mathrm{I}_{2}, \mathrm{I}_{4}<50 \mu \mathrm{~A}$ and linearity decreases when $\mathrm{I}_{1}, \mathrm{I}_{2}, \mathrm{I}_{4}>$ $250 \mu \mathrm{~A}$ (e.g., @ $\mathrm{I}_{1}=\mathrm{I}_{2}=500 \mu \mathrm{~A}$ nonlinearity error $\approx 0.5 \%$ ).
2. This section will not deal with feedthrough which is proportional to frequency of operation and caused by stray capacitance and/or bandwidth limitations. (refer to Figure 12.)
3. Not including resistor tolerance or output offset on the operational amplifier.
4. For $50 \mu \mathrm{~A} \leq \mathrm{I}_{1}, \mathrm{I}_{2}, \mathrm{I}_{4} \leq 250 \mu \mathrm{~A}$.

## Errors Caused by Input Offsets



System errors can be greatly reduced by externally trimming the input offset voltages of the RC4200. ( $\pm 3.0 \%$ F.S. for RC4200 and $\pm 0.1 \%$ for RC4200A.)


65-1870
If Xos $=\mathrm{XOSX}, \mathrm{YOS}=\mathrm{YOSY}, \mathrm{ZOS}=-\mathrm{VOSZ}$,

$$
\text { then } \mathrm{V}_{\mathrm{O}} \frac{\mathrm{~V}_{\mathrm{X}} \mathrm{~V}_{\mathrm{Y}}}{\mathrm{~V}_{\mathrm{Z}}} \frac{\mathrm{R}_{0} \mathrm{R}_{4}}{\mathrm{R}_{1} \mathrm{R}_{2}} \pm 0.3 \% \text { F.S.) }
$$

Figure 13. RC4200 with Input Offset Adjustment

## Extended Range Circuit Errors

The extended range configurations have a disadvantage in that additional accuracy errors may be introduced by resistor product mismatching.

## Multiplier

An error in resistor product matching will cause an equivalent feedthrough or output offset error. See Figure 6.
$\mathrm{R}_{1} \mathrm{R}_{\mathrm{b}}=\mathrm{R}_{\mathrm{CX}} \mathrm{R}_{\mathrm{d}} \pm \alpha, \mathrm{V}_{\mathrm{X}}$ feedthrough $\left(\mathrm{V}_{\mathrm{Y}}=0\right)=\mathrm{I} \alpha \mathrm{V}_{\mathrm{X}}$
$\mathrm{R}_{2} \mathrm{Ra}_{\mathrm{a}}=\mathrm{R}_{\mathrm{CY}} \mathrm{R}_{\mathrm{d}} \pm \beta, \mathrm{V}_{\mathrm{Y}}$ feedthrough $\left(\mathrm{V}_{\mathrm{X}}=0\right)= \pm \beta \mathrm{V}_{\mathrm{Y}}$
$\mathrm{Ra}_{\mathrm{a}} \mathrm{Rb}_{\mathrm{b}}=\mathrm{RCR}_{\mathrm{d}} \pm \gamma, \mathrm{V}_{0}$ offset $\left(\mathrm{VX}=\mathrm{V}_{\mathrm{Y}}=0\right)= \pm \gamma \mathrm{VREF}^{*}$

## Note:

* Output offset errors can always be trimmed out with the output op amp offset adjust, VOS (R16).


## Reducing Mismatch Errors

You need not use $0.01 \%$ resistors to reduce resistor product mismatch errors. Here are a couple of ways to obtain maximum accuracy out of the extended range multiplier (see Figure 4) using 1\% resistors.

## Method 1

$\mathrm{V}_{\mathrm{X}}$ feedthrough, for example, occurs when $\mathrm{VY}=0$ and VOSY $\neq 0$. This $V_{X}$ feedthrough will equal $\pm V_{X V O S Y}$. Also, if VOSZ $\neq 0$, there is a $V_{X}$ feedthrough equal to $\mathrm{V}_{\mathrm{X}}$ VosZ. A resistor-product error of $\alpha$ will cause a $\mathrm{V}_{\mathrm{X}}$ feedthrough of $\pm \alpha V_{X}$. Likewise, $V_{Y}$ feedthrough errors are: $\pm \mathrm{V}_{Y}$ VOSX, $\pm \mathrm{V}_{Y}$ VosZ and $\pm \beta \mathrm{V}_{Y}$

Total feedthrough:
$\pm \mathrm{V}_{\mathrm{X}} \mathrm{V}_{\text {OSY }} \pm \mathrm{V}_{\mathrm{Y}} \mathrm{V}_{\text {OSX }} \pm \alpha \mathrm{VX} \pm \beta \mathrm{VY} \pm(\mathrm{VX}+\mathrm{VY})$ VOSZ
By carefully abusing $\operatorname{XOS}(\mathrm{R} 5), \operatorname{YOS}(\mathrm{R} 9)$ and $\operatorname{ZOS}(\mathrm{R} 20)$ this equation can be made to very nearly equal zero and the feedthrough error will practically disappear.

A residual of set will probably remain which can be trimmed outwith $\operatorname{VOS}\left(\mathrm{R}_{16}\right)$ at the output of amp.

## Method 2

Notice that the ratios of $R_{1} R_{b}: R_{C X} R_{d}$ and $R_{2} R_{a}: R_{C Y} R_{d}$ are both dependent of $R_{d}$ also that $R_{1}, R_{2}, R_{a}$ and $R_{b}$ are all functions of the maximum input requirements. By designing a multiplier for the same input ranges on both $V_{X}$ and $V_{Y}$ then $R_{1}=R_{2}, R_{C X}=R_{C Y}$ and $R_{a}=R_{b}$. (Note: it is acceptable to design a four quadrant multiplier and use only two quadrants of it.)

Select $\mathrm{R}_{\mathrm{d}}$ to be $1 \%$ or $2 \%$ below (or above) the calculated value. This will cause $\alpha$ and $\beta$ to both be positive (or negative) by nearly the same amount. Now the effective value of $\mathrm{R}_{\mathrm{d}}$ can be trimmed with an offset adjustment $\operatorname{ZOS}\left(\mathrm{R}_{20}\right)$ on pin 5.

This technique causes: a slight gain error which can be compensated with the R0 value, and an output of offset error that can be trimmed with $\operatorname{VOS}(\mathrm{R} 16)$ on the output op amp.

## Extended Range Divider

The only cross-product error of interest is the $\mathrm{V} Z$ feedthrough ( $\mathrm{VX}=0$ and $\operatorname{VOSX} \neq 0$ ) which is easily adjusted with Xos(R5). See Figure 6.

Resistor product mismatch will cause scaling errors (gain) that could be a problem for very low values of VZ. Adjustments to $\operatorname{YOS}\left(\mathrm{R}_{18}\right)$ can be made to improve the high gain accuracy.

## Square Root and Squaring

These circuits are functions of single variables so feedthrough, as such, is not a consideration. Cross product errors will effect incremental accuracy that can be corrected $\operatorname{YOS}\left(\mathrm{R}_{14}\right)$ or $\operatorname{ZOS}\left(\mathrm{R}_{10}\right)$. See Figure 9 and Figure 11.

## Appendix 2—Applications

Design Considerations for RMS-to-DC Circuits

## Average Value

Consider Vin $=$ Asin $\omega \tau$. By definition,
$\mathrm{V}_{\mathrm{AG}}=\int_{0}^{\frac{\mathrm{T}}{2}} \mathrm{~V}_{\mathrm{IN}} \mathrm{dt}$
Where $\mathrm{T}=$ Period

$$
\begin{aligned}
\omega & =2 \pi f \\
& =\frac{2 \pi}{T}
\end{aligned}
$$


$\mathrm{V}_{\mathrm{AG}}=\frac{2}{\mathrm{~T}} \int_{0}^{\frac{\mathrm{T}}{2}} \mathrm{~A} \sin \omega \mathrm{tdt}$

$$
\begin{aligned}
& =\frac{2 \mathrm{~A}}{\mathrm{~T}}\left[-\frac{1}{\omega} \cos \omega \mathrm{t}\right]_{0}^{\frac{\mathrm{T}}{2}} \\
& =\frac{2 \mathrm{~A}}{2 \pi}[-\cos (\pi)+\cos (0)]
\end{aligned}
$$

Average Value of $\mathrm{A} \sin \omega t$ is $\frac{2}{\pi} \mathrm{~A}$

## RMS Value

Again, consider VIN $=$ Asin $\omega t$
$\mathrm{V}_{\mathrm{rms}}=\sqrt{\mathrm{V}_{\mathrm{AVG}}}=\sqrt{\frac{1}{\mathrm{~T}} \int_{0}^{\mathrm{T}}\left[\mathrm{V}_{\mathrm{IN}}\right]^{2} \mathrm{dt}}$
$\mathrm{V}_{\mathrm{rms}}$ for $\mathrm{Asin} \omega \mathrm{tdt}$ :
$V_{r m s}=\sqrt{\frac{1}{T} \int_{0}^{T} A^{2} \sin ^{2} \omega t d t}$
$\mathrm{V}_{\mathrm{rms}}=\sqrt{\frac{\mathrm{A}^{2}}{\mathrm{~T}} \int_{0}^{\mathrm{T}}\left[\frac{1}{2}-\frac{1}{2} \cos 2 \cos 2 \omega \mathrm{t}\right] \mathrm{dt}}$
$\mathrm{V}_{\mathrm{rms}}=\sqrt{\frac{\mathrm{A}^{2}}{2}\left[\frac{\mathrm{~T}}{2}-\frac{1}{4 \omega} \sin 2 \omega \mathrm{t}\right]_{0}^{\mathrm{T}}}$
$\mathrm{V}_{\mathrm{rms}}=\sqrt{\frac{\mathrm{A}^{2}}{2}\left[\frac{\mathrm{~T}}{2}\right]}$
$\mathrm{V}_{\mathrm{rms}}=\sqrt{\frac{\mathrm{A}^{2}}{2}}$

Therefore, the rms value of Asin$\omega t$ becomes:
$\mathrm{V}_{\mathrm{rms}}=\frac{\mathrm{A}}{\sqrt{2}}$
RMS Value for Rectified Sine Waves
Consider $\mathrm{V}_{\text {in }}=|\mathrm{A} \sin \omega \mathrm{t}|$, a rectified wave. To solve, integrate of each half cycle.
i.e. $\frac{1}{\mathrm{~T}} \int_{0} \mathrm{TV}_{\mathrm{in}}^{2} \mathrm{dt}=$ $\frac{1}{T}\left[\int_{0}^{\frac{T}{2}} A^{2} \sin ^{2} \omega t d t+\int_{\frac{T}{2}}^{T}(-A \sin \omega t)^{2} d t\right]$

This is the same as $\frac{1}{1} \int_{0} \mathrm{TA}^{2} \sin ^{2} \omega \mathrm{tdt}$ $\mathrm{so},|\mathrm{Asin} \omega \mathrm{t}|_{\mathrm{rms}}=\mathrm{A} \sin \omega \mathrm{t}_{\mathrm{rms}}$

Practical Consideration: IAsin $\omega t \mid$ has high-order harmonics; Asin $\omega t$ does not. Therefore, non-ideal integrators may cause different errors for two approaches.
(a)


Figure 14.
$\operatorname{Avg}\left[\frac{\mathrm{V}_{\mathrm{IN}}^{2}}{\mathrm{~V}_{0}}\right]=\mathrm{V}_{0}$
implies $\mathrm{V}_{0}=\sqrt{\operatorname{Avg}\left(\left|\mathrm{V}_{\mathrm{IN}}{ }^{2}\right|\right)}$
$\mathrm{V}_{0}=\sqrt{\operatorname{Avg} \mathrm{V}_{\mathrm{IN}}}{ }^{2}$


Figure 15. RMS to DC Converter VouT $=\sqrt{ } \mathbf{V I N}^{2}$

## Amplitude Modulator with A.G.C.

In many AC modulator applications, unwanted output modulation is caused by variations in carrier input amplitude. The versatility of the RC4200 multiplier can be utilizes to eliminate this undesired fluctuation. The extended range multiplier circuit (Figure 4) shows an output amplitude inversely proportional to the reference voltage VREF.
i.e., $V_{0}=\frac{V_{X} V_{Y}}{V_{\text {REF }}} \frac{R_{0} R_{d}}{R_{1} R_{2}}$

By making $\mathrm{V}_{\text {REF }}$ proportional to $\mathrm{V}_{\mathrm{Y}}$ (where $\mathrm{V}_{\mathrm{Y}}$ is the carrier input) such that:
$\mathrm{V}_{\text {REF }}=\mathrm{V}_{\mathrm{H}}=\int\left(\left|\mathrm{V}_{\mathrm{Y}}\right|\right)$
Then the denominator becomes a variable value that automatically provides constant gain, such that the modulating input ( $\mathrm{V}_{\mathrm{X}}$ ) modulates the carrier ( VY ) with a fixed scale factor even though the carrier varies in amplitude.

If $\mathrm{V}_{\mathrm{H}}$ is made proportional to the average value of $\mathrm{A} \sin \omega \mathrm{t}$ (i.e., $2 \mathrm{~A} / \pi$ ) and scaled by a value of $\pi / 2$ then:
$\mathrm{V}_{\mathrm{H}}=\mathrm{A}$
and if: $\mathrm{VX}=$ Modulating input $(\mathrm{VM})$
and: VY Carrier input (Asin $\omega t$ )
Then: $\mathrm{V}_{0}=K \mathrm{~V}_{\mathrm{M}} \sin \omega \mathrm{t}$ where $\mathrm{K}=\frac{\mathrm{R}_{0} \mathrm{R}_{\mathrm{d}}}{\mathrm{R}_{1} \mathrm{R}_{2}}$
The resistor scaling is determined by the dynamic range of the carrier variation and modulating input.

The resistor values are solved, as with the other extended range circuits, in terms of the input voltages.

Input voltages:
Modulation voltage $\left(\mathrm{V}_{\mathrm{M}}\right): 0 \leq \mathrm{V}_{\mathrm{M}} \leq \mathrm{V}_{\mathrm{X}}(\max$.
Carrier ( $\mathrm{V}_{\mathrm{Y}}$ ): $\mathrm{V}_{\mathrm{Y}}=\mathrm{Asin} \omega \mathrm{t}$
Carrier amplitude fluctuation ( $\Delta \mathrm{A}$ ):
A (min.) $\operatorname{sint} \leq \mathrm{V}_{\mathrm{Y}} \leq \mathrm{A}($ max. $) \sin \Omega \omega t$
Dynamic Range (N): A(max.)/A(min.),
$\mathrm{A}(\max )=.\mathrm{V}_{\mathrm{H}}(\max$.$) and \mathrm{A}(\min )=.\mathrm{V}_{\mathrm{H}}(\min$.


Figure 16. Amplitude Modulator with A.G.C.

The maximum and minimum values for $\mathrm{I}_{1}$ and $\mathrm{I}_{2}$ lead to:

$$
\begin{aligned}
& \mathrm{I}_{1}(\max .)=\frac{\mathrm{V}_{\mathrm{X}}(\text { max. })}{\mathrm{R}_{1}}+\frac{\mathrm{V}_{\mathrm{H}}(\text { max. })}{\mathrm{R}_{\mathrm{a}}}=250 \mu \mathrm{~A} \\
& \mathrm{I}_{1}(\min .)=\frac{\mathrm{V}_{\mathrm{H}}(\min .)}{\mathrm{R}_{\mathrm{a}}}=50 \mu \mathrm{~A} \mathrm{~V}_{\mathrm{M}}(\min .)=0 \\
& \mathrm{I}_{2}(\max .)=\frac{\mathrm{A}(\max .)}{\mathrm{R}_{2}}+\frac{\mathrm{V}_{\mathrm{H}}(\text { max. })}{\mathrm{R}_{\mathrm{a}}}=250 \mu \mathrm{~A} \\
& \mathrm{I}_{2}(\min .)=\frac{\mathrm{V}_{\mathrm{H}}(\min .)}{\mathrm{R}_{\mathrm{a}}}=50 \mu \mathrm{~A}
\end{aligned}
$$

For a dynamic range of N , where

$$
\mathrm{N}=\frac{\mathrm{A}(\max .)}{\mathrm{A}(\min .)}<5,
$$

These equations combine to yield:

$$
\begin{aligned}
& \mathrm{R}_{1}=\frac{\mathrm{V}_{\mathrm{X}}(\max .)}{(5-\mathrm{N}) 50 \mu \mathrm{~A}}, \mathrm{R} 2 \frac{\mathrm{~A}(\max .)}{(5-\mathrm{N}) 50 \mu \mathrm{~A}} \\
& \mathrm{R}_{\mathrm{a}}=\frac{\mathrm{A}(\min .)}{50 \mu \mathrm{~A}} \text { and } \mathrm{R}_{\mathrm{O}}=\mathrm{K} \frac{\mathrm{R}_{1} \mathrm{R}_{2}}{\mathrm{R}_{\mathrm{a}}}
\end{aligned}
$$

Example 1
$\mathrm{V}_{\mathrm{Y}}=\mathrm{A} \sin \omega \mathrm{t} 2.5 \mathrm{~V} \leq \mathrm{A} \leq 10 \mathrm{~V}$, therefore $\mathrm{N}=4$
$0 \mathrm{~V} \leq \mathrm{VM}_{\mathrm{M}} \leq 10 \mathrm{~V}$, therefore $\mathrm{VX}_{\mathrm{X}}($ max. $)=10 \mathrm{~V}$
$\mathrm{K}=1$, therefore $\mathrm{V}_{0}=\mathrm{VM}_{\mathrm{M}} \sin \omega \mathrm{t}$

$$
\begin{aligned}
& \mathrm{R}_{1}=\frac{\mathrm{V}_{\mathrm{X}}(\text { max. })}{50 \mu \mathrm{~A}}=\frac{10 \mathrm{~V}}{50 \mu \mathrm{~A}}=200 \mathrm{~K} \\
& \mathrm{R}_{1}=\frac{\mathrm{A}(\text { max. })}{50 \mu \mathrm{~A}}=\frac{10 \mathrm{~V}}{50 \mu \mathrm{~A}}=200 \mathrm{~K} \\
& \mathrm{R}_{\mathrm{a}}=\frac{\mathrm{A}(\mathrm{~min} .)}{50 \mu \mathrm{~A}}=\frac{2.5 \mathrm{~V}}{50 \mu \mathrm{~A}}=50 \mathrm{~K} \\
& \mathrm{R}_{\mathrm{O}}=\mathrm{K} \frac{\mathrm{R}_{1} \mathrm{R}_{2}}{\mathrm{R}_{\mathrm{a}}}=1 \frac{200 \mathrm{~K} \times 200 \mathrm{~K}}{50 \mathrm{~K}}=800 \mathrm{~K}
\end{aligned}
$$

## Example 2

$\mathrm{VY}=\mathrm{A} \sin \omega \mathrm{t} 3 \leq \mathrm{A} \leq 6$, therefore $\mathrm{N}=2$
$0 \mathrm{~V} \leq \mathrm{V}_{\mathrm{M}} \leq 8 \mathrm{~V}$, therefore $\mathrm{VX}_{\mathrm{X}}$ (max. $)=8 \mathrm{~V}$
$\mathrm{K}=0.2$, therefore $\mathrm{V}_{0}=0.2 \mathrm{Vm}_{\mathrm{M}}$ sinwt
so:
$\mathrm{R}_{1}=53.3 \mathrm{~K}, \mathrm{R}_{2}=40 \mathrm{~K}$
$\mathrm{R}_{\mathrm{a}}=60 \mathrm{~K}$ and $\mathrm{R}_{0}=7.11 \mathrm{~K}$


## Limited Range, First Quadrant Applications

The following circuit has the advantage that cross-product errors are due only to input offsets and nonlinearity error is sightly error is slightly less for lower input currents.

The circuit also has no standby current to add to the noise content, although the signal-to-noise ratio worsens at very low input currents $(1-5 \mu \mathrm{~A})$ due to the noise current of the input stages.

The RSCs filter circuits are added to each input to improve the stability for input currents below $50 \mu \mathrm{~A}$.

## Caution!

The bandpass drops off significantly for lower currents $(<50 \mu \mathrm{~A})$ and non-symmetrical rise and fall times can cause second harmonic distortion.

Thermal Symmetry


The scale factor is sensitive to temperature gradients across the chip in the lateral direction. Where possible, the package should be oriented such that forces generating temperature gradients are located physically on the line of thermal symmetry. This will minimize scale-factor error due to thermal gradients.






Figure 18. Outputs


Figure 19a. Output Noise Current ( $\mathrm{I}_{3}$ ) vs. Input Currents ( $\mathrm{I}_{1}, \mathrm{I}_{2}$ ) for $\mathrm{I}_{\mathbf{4}}=\mathbf{2 5 0} \boldsymbol{\mu} \mathrm{A}$


Figure 19b. Output Noise Current (l3) vs. Input Currents ( $\mathrm{I}_{4}, \mathrm{I}_{1}$ ) for $\mathrm{I}_{\mathbf{2}}=\mathbf{2 5 0} \boldsymbol{\mu} \mathrm{A}$


Figure 20. AC Feedthrough vs. Frequency

## Mechanical Dimensions

## 8-Lead SOIC Package

| Symbol | Inches |  | Millimeters |  | Notes |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | Min. | Max. | Min. | Max. |  |
| A | .053 | .069 | 1.35 | 1.75 |  |
| A1 | .004 | .010 | 0.10 | 0.25 |  |
| B | .013 | .020 | 0.33 | 0.51 |  |
| C | .008 | .010 | 0.20 | 0.25 | 5 |
| D | .189 | .197 | 4.80 | 5.00 | 2 |
| E | .150 | .158 | 3.81 | 4.01 | 2 |
| e | .050 BSC |  | 1.27 BSC |  |  |
| H | .228 | .244 | 5.79 | 6.20 |  |
| h | .010 | .020 | 0.25 | 0.50 |  |
| L | .016 | .050 | 0.40 | 1.27 | 3 |
| N | 8 |  |  |  | 8 |
| $\alpha$ | $0^{\circ}$ | $8^{\circ}$ | $0^{\circ}$ | $8^{\circ}$ | 6 |
| ccc | - | .004 | - | 0.10 |  |

## Notes:

1. Dimensioning and tolerancing per ANSI Y14.5M-1982.
2. "D" and "E" do not include mold flash. Mold flash or protrusions shall not exceed .010 inch ( 0.25 mm ).
3. "L" is the length of terminal for soldering to a substrate.
4. Terminal numbers are shown for reference only.
5. "C" dimension does not include solder finish thickness.
6. Symbol " N " is the maximum number of terminals.


Mechanical Dimensions (continued)

## 8-Lead Plastic DIP Package

| Symbol | Inches |  | Millimeters |  | Notes |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | Min. | Max. | Min. | Max. |  |
| A | - | .210 | - | 5.33 |  |
| A1 | .015 | - | .38 | - |  |
| A2 | .115 | .195 | 2.93 | 4.95 |  |
| B | .014 | .022 | .36 | .56 |  |
| B1 | .045 | .070 | 1.14 | 1.78 |  |
| C | .008 | .015 | .20 | .38 | 4 |
| D | .348 | .430 | 8.84 | 10.92 | 2 |
| D1 | .005 | - | .13 | - |  |
| E | .300 | .325 | 7.62 | 8.26 |  |
| E1 | .240 | .280 | 6.10 | 7.11 | 2 |
| e | .100 BSC | 2.54 BSC |  |  |  |
| eB | - | .430 | - | 10.92 |  |
| L | .115 | .160 | 2.92 | 4.06 |  |
| N | $8^{\circ}$ |  |  | $8^{\circ}$ |  |

## Notes:

1. Dimensioning and tolerancing per ANSI Y14.5M-1982.
2. "D" and "E1" do not include mold flashing. Mold flash or protrusions shall not exceed .010 inch ( 0.25 mm ).
3. Terminal numbers are for reference only.
4. " C " dimension does not include solder finish thickness.
5. Symbol " N " is the maximum number of terminals.


## Ordering Information

| Part Number | Package | Operating Temperature Range |
| :---: | :---: | :---: |
| RC4200N | 8-Lead Plastic DIP | $0^{\circ} \mathrm{C}$ to $+70^{\circ} \mathrm{C}$ |
| RC4200AN | 8-Lead Plastic DIP | $0^{\circ} \mathrm{C}$ to $+70^{\circ} \mathrm{C}$ |
| RC4200M | 8-Lead SOIC | $0^{\circ} \mathrm{C}$ to $+70^{\circ} \mathrm{C}$ |
| RC4200AM | 8-Lead SOIC | $0^{\circ} \mathrm{C}$ to $+70^{\circ} \mathrm{C}$ |

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