## MC14560B

## NBCD Adder

The MC14560B adds two 4-bit numbers in NBCD (natural binary coded decimal) format, resulting in sum and carry outputs in NBCD code.

This device can also subtract when one set of inputs is complemented with a 9's Complementer (MC14561B).

All inputs and outputs are active high. The carry input for the least significant digit is connected to $V_{S S}$ for no carry in.

- Diode Protection on All Inputs
- Supply Voltage Range = 3.0 Vdc to 18 Vdc
- Capable of Driving Two Low-power TTL Loads or One Low-power Schottky TTL Load Over the Rated Temperature Range

MAXIMUM RATINGS* (Voltages Referenced to $\mathrm{V}_{\text {SS }}$ )

| Symbol | Parameter | Value | Unit |
| :---: | :--- | :---: | :---: |
| $\mathrm{V}_{\mathrm{DD}}$ | DC Supply Voltage | -0.5 to +18.0 | V |
| $\mathrm{~V}_{\text {in }}, \mathrm{V}_{\text {out }}$ | Input or Output Voltage (DC or Transient) | -0.5 to $\mathrm{V}_{\mathrm{DD}}+0.5$ | V |
| $\mathrm{I}_{\text {in }}, \mathrm{I}_{\text {out }}$ | Input or Output Current (DC or Transient), <br> per Pin | $\pm 10$ | mA |
| $\mathrm{P}_{\mathrm{D}}$ | Power Dissipation, per Package $\dagger$ | 500 | mW |
| $\mathrm{~T}_{\mathrm{stg}}$ | Storage Temperature | -65 to +150 | ${ }^{\circ} \mathrm{C}$ |
| $\mathrm{T}_{\mathrm{L}}$ | Lead Temperature (8-Second Soldering) | 260 | ${ }^{\circ} \mathrm{C}$ |

* Maximum Ratings are those values beyond which damage to the device may occur. $\dagger$ Temperature Derating:

Plastic "P and D/DW" Packages: $-7.0 \mathrm{~mW} /{ }^{\circ} \mathrm{C}$ From $65^{\circ} \mathrm{C}$ To $125^{\circ} \mathrm{C}$
Ceramic "L" Packages: $-12 \mathrm{~mW} /{ }^{\circ} \mathrm{C}$ From $100^{\circ} \mathrm{C}$ To $125^{\circ} \mathrm{C}$
TRUTH TABLE*

| Input |  |  |  |  |  |  |  |  | Output |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A4 | A3 | A2 | A1 | B4 | B3 | B2 | B1 | $\mathrm{C}_{\text {in }}$ | Cout | S4 | S3 | S2 | S1 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 1 |
| 0 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 |

* Partial truth table to show logic operation for representative input values.

This device contains protection circuitry to guard against damage due to high static voltages or electric fields. However, precautions must be taken to avoid applications of any voltage higher than maximum rated voltages to this high-impedance circuit. For proper operation, $\mathrm{V}_{\text {in }}$ and $\mathrm{V}_{\text {out }}$ should be constrained to the range $\mathrm{V}_{\mathrm{SS}} \leq\left(\mathrm{V}_{\text {in }}\right.$ or $\left.\mathrm{V}_{\text {out }}\right) \leq \mathrm{V}_{\text {DD }}$.

Unused inputs must always be tied to an appropriate logic voltage level (e.g., either $\mathrm{V}_{\mathrm{SS}}$ or $\mathrm{V}_{\mathrm{DD}}$ ). Unused outputs must be left open.


L SUFFIX
CERAMIC CASE 620


D SUFFIX
SOIC
CASE 751B
ORDERING INFORMATION

| MC14XXXBCP | Plastic |
| :--- | :--- |
| MC14XXXBCL | Ceramic |
| MC14XXXBD | SOIC |

$\mathrm{T}_{\mathrm{A}}=-55^{\circ}$ to $125^{\circ} \mathrm{C}$ for all packages.


ELECTRICAL CHARACTERISTICS (Voltages Referenced to $V_{S S}$ )

| Characteristic | Symbol | $\begin{aligned} & \text { VDD } \\ & \text { Vdc } \end{aligned}$ | $-55^{\circ} \mathrm{C}$ |  | $25^{\circ} \mathrm{C}$ |  |  | $125^{\circ} \mathrm{C}$ |  | Unit |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Min | Max | Min | Typ \# | Max | Min | Max |  |
| $\left.\begin{array}{cc}\text { Output Voltage } \\ V_{\text {in }}=V_{D D} \text { or } 0 & \text { "0" Level } \\ & \\ & \\ V_{\text {in }}=0 \text { or } V_{D D} & \text { " } 1 " \text { Level }\end{array}\right]$ | V OL | $\begin{aligned} & \hline 5.0 \\ & 10 \\ & 15 \end{aligned}$ | - | $\begin{aligned} & 0.05 \\ & 0.05 \\ & 0.05 \end{aligned}$ | - | 0 0 0 | $\begin{aligned} & 0.05 \\ & 0.05 \\ & 0.05 \end{aligned}$ | - | $\begin{aligned} & \hline 0.05 \\ & 0.05 \\ & 0.05 \end{aligned}$ | Vdc |
|  | $\mathrm{V}_{\mathrm{OH}}$ | $\begin{aligned} & \hline 5.0 \\ & 10 \\ & 15 \end{aligned}$ | $\begin{gathered} \hline 4.95 \\ 9.95 \\ 14.95 \end{gathered}$ | - | $\begin{gathered} \hline 4.95 \\ 9.95 \\ 14.95 \end{gathered}$ | $\begin{aligned} & \hline 5.0 \\ & 10 \\ & 15 \end{aligned}$ | - | $\begin{gathered} \hline 4.95 \\ 9.95 \\ 14.95 \end{gathered}$ | - | Vdc |
| Input Voltage $\quad$ " 0 " Level <br> $\left(\mathrm{V}_{\mathrm{O}}=4.5\right.$ or 0.5 Vdc$)$ <br> $\left(\mathrm{V}_{\mathrm{O}}=9.0\right.$ or 1.0 Vdc$)$ <br> $\left(\mathrm{V}_{\mathrm{O}}=13.5\right.$ or 1.5 Vdc$)$ <br>  <br>  <br> $\left(\mathrm{V}_{\mathrm{O}}=0.5\right.$ or 4.5 Vdc$)$ <br> $\left(\mathrm{V}_{\mathrm{O}}=1.0\right.$ or 9.0 Vdc$)$ <br> $\left(\mathrm{V}_{\mathrm{O}}=1.5\right.$ or 13.5 Vdc$)$ | $\mathrm{V}_{\mathrm{IL}}$ | 5.0 10 15 | 二 | $\begin{aligned} & 1.5 \\ & 3.0 \\ & 4.0 \end{aligned}$ | 二 | $\begin{aligned} & 2.25 \\ & 4.50 \\ & 6.75 \end{aligned}$ | 1.5 3.0 4.0 | - | $\begin{aligned} & 1.5 \\ & 3.0 \\ & 4.0 \end{aligned}$ | Vdc |
|  | $\mathrm{V}_{\mathrm{IH}}$ | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | 3.5 7.0 11 | - | $\begin{aligned} & 3.5 \\ & 7.0 \\ & 11 \end{aligned}$ | $\begin{aligned} & 2.75 \\ & 5.50 \\ & 8.25 \end{aligned}$ | - | $\begin{aligned} & 3.5 \\ & 7.0 \\ & 11 \end{aligned}$ | - | Vdc |
| Output Drive Current  <br> $(\mathrm{VOH}=2.5 \mathrm{Vdc})$ Source <br> $(\mathrm{VOH}=4.6 \mathrm{Vdc})$  <br> $(\mathrm{VOH}=9.5 \mathrm{Vdc})$  <br> $(\mathrm{VOH}=13.5 \mathrm{Vdc})$  | ${ }^{\mathrm{IOH}}$ | $\begin{aligned} & 5.0 \\ & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | $\begin{gathered} -3.0 \\ -0.64 \\ -1.6 \\ -4.2 \end{gathered}$ | - | $\begin{gathered} -2.4 \\ -0.51 \\ -1.3 \\ -3.4 \end{gathered}$ | $\begin{gathered} -4.2 \\ -0.88 \\ -2.25 \\ -8.8 \end{gathered}$ | - | $\begin{gathered} -1.7 \\ -0.36 \\ -0.9 \\ -2.4 \end{gathered}$ | - | mAdc |
| $\begin{array}{ll} (\mathrm{VOL}=0.4 \mathrm{Vdc}) & \text { Sink } \\ (\mathrm{VOL}=0.5 \mathrm{Vdc}) & \\ \left(\mathrm{V}_{\mathrm{OL}}=1.5 \mathrm{Vdc}\right) & \end{array}$ | IOL | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | $\begin{gathered} \hline 0.64 \\ 1.6 \\ 4.2 \end{gathered}$ | - | $\begin{gathered} \hline 0.51 \\ 1.3 \\ 3.4 \end{gathered}$ | $\begin{gathered} \hline 0.88 \\ 2.25 \\ 8.8 \end{gathered}$ | - | $\begin{gathered} \hline 0.36 \\ 0.9 \\ 2.4 \end{gathered}$ | - | mAdc |
| Input Current | $\mathrm{l}_{\text {in }}$ | 15 | - | $\pm 0.1$ | - | $\pm 0.00001$ | $\pm 0.1$ | - | $\pm 1.0$ | $\mu \mathrm{Adc}$ |
| Input Capacitance $\left(\mathrm{V}_{\mathrm{in}}=0\right)$ | $\mathrm{C}_{\text {in }}$ | - | - | - | - | 5.0 | 7.5 | - | - | pF |
| Quiescent Current (Per Package) | IDD | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | - | $\begin{aligned} & 5.0 \\ & 10 \\ & 20 \end{aligned}$ | - | $\begin{aligned} & 0.005 \\ & 0.010 \\ & 0.015 \end{aligned}$ | 5.0 10 20 | - | $\begin{aligned} & 150 \\ & 300 \\ & 600 \end{aligned}$ | $\mu \mathrm{Adc}$ |
| Total Supply Current** $\dagger$ <br> (Dynamic plus Quiescent, Per Package) ( $C_{L}=50 \mathrm{pF}$ on all outputs, all buffers switching) | ${ }^{1} \mathrm{~T}$ | $\begin{aligned} & \hline 5.0 \\ & 10 \\ & 15 \end{aligned}$ | $\begin{aligned} & \mathrm{IT}=(1.68 \mu \mathrm{~A} / \mathrm{kHz}) \mathrm{f}+\mathrm{I} \mathrm{DD} \\ & \mathrm{IT}=(3.35 \mu \mathrm{~A} / \mathrm{kHz}) \mathrm{f}+\mathrm{IDD} \\ & \mathrm{I} \mathrm{D}=(5.03 \mu \mathrm{~A} / \mathrm{kHz}) \mathrm{f}+\mathrm{I} \mathrm{DD} \end{aligned}$ |  |  |  |  |  |  | $\mu \mathrm{Adc}$ |

\#Data labelled "Typ" is not to be used for design purposes but is intended as an indication of the IC's potential performance.
${ }^{* *}$ The formulas given are for the typical characteristics only at $25^{\circ} \mathrm{C}$.
$\dagger$ To calculate total supply current at loads other than 50 pF :

$$
I_{T}\left(C_{L}\right)=I_{T}(50 \mathrm{pF})+\left(C_{L}-50\right) \mathrm{Vfk}
$$

where: $I_{T}$ is in $\mu \mathrm{A}$ (per package), $\mathrm{C}_{\mathrm{L}}$ in $\mathrm{pF}, \mathrm{V}=\left(\mathrm{V}_{\mathrm{DD}}-\mathrm{V}_{\mathrm{SS}}\right)$ in volts, f in kHz is input frequency, and $\mathrm{k}=0.005$.

PIN ASSIGNMENT

| $1 \bullet$ | 16 |
| :---: | :---: |
| 2 | 15 |
| 3 | 14 |
| 4 | 13 |
| 5 | 12 |
| 6 | 11 |
| 7 | 10 |
| 8 | 9 |

SWITCHING CHARACTERISTICS* $\left(C_{L}=50 \mathrm{pF}, \mathrm{T}_{\mathrm{A}}=25^{\circ} \mathrm{C}\right)$

| Characteristic | Symbol | VDD | Min | Typ \# | Max | Unit |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Output Rise and Fall Time } \\ & \text { t } \mathrm{TLH}, \mathrm{t} \mathrm{THL}=(1.5 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+25 \mathrm{~ns} \\ & \text { t } \mathrm{TLH}, \mathrm{t} \mathrm{tHL}=(0.75 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+12.5 \mathrm{~ns} \\ & \text { t } \mathrm{TLH}, \mathrm{t} \mathrm{tHL}=(0.55 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+9.5 \mathrm{~ns} \end{aligned}$ | ${ }_{\text {t }}$ LH, ${ }^{\text {t }}$ THL | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | - | $\begin{gathered} 100 \\ 50 \\ 40 \end{gathered}$ | $\begin{gathered} 200 \\ 100 \\ 80 \end{gathered}$ | ns |
| ```Propagation Delay Time A or B to S tPLH, tPHL = (1.7 ns/pF) CL + 665 ns tPLH, tPHL = (0.66 ns/pF) CL + 297 ns tPLH, tPHL = (0.5 ns/pF) CL + 195 ns``` | ${ }_{\text {tPLH, }}$ tPHL | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | - | $\begin{aligned} & 750 \\ & 330 \\ & 220 \end{aligned}$ | $\begin{gathered} 2100 \\ 900 \\ 675 \end{gathered}$ | ns |
| $\begin{aligned} & \text { A or B to } C_{\text {out }} \\ & \text { tPLH, } \\ & \text { tPLH, } \mathrm{tPHL}=(1.7 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+565 \mathrm{~ns} \\ & \text { tPLH, } \end{aligned}$ |  | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | - | $\begin{aligned} & 650 \\ & 230 \\ & 170 \end{aligned}$ | $\begin{aligned} & 1800 \\ & 600 \\ & 450 \end{aligned}$ | ns |
| $\begin{aligned} & \mathrm{C}_{\text {in }} \text { to } \mathrm{C}_{\text {out }} \\ & \text { tPLH, tPHL }=(1.7 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+465 \mathrm{~ns} \\ & \text { tPLH, tPHL }=(0.66 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+187 \mathrm{~ns} \\ & \text { tpLH, tPHL }=(0.5 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+135 \mathrm{~ns} \end{aligned}$ |  | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ |  | $\begin{aligned} & 550 \\ & 220 \\ & 160 \end{aligned}$ | $\begin{aligned} & 1500 \\ & 600 \\ & 450 \end{aligned}$ | ns |
| Turn-Off Delay Time <br> Cin to $S$ <br> tPLH $=(1.7 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+715 \mathrm{~ns}$ <br> tPLH $=(0.66 \mathrm{~ns} / \mathrm{pF}) \mathrm{CL}_{\mathrm{L}}+197 \mathrm{~ns}$ <br> tPLH $=(0.5 \mathrm{~ns} / \mathrm{pF}) \mathrm{C}_{\mathrm{L}}+215 \mathrm{~ns}$ | tPLH | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | - | $\begin{aligned} & 800 \\ & 350 \\ & 240 \end{aligned}$ | $\begin{gathered} 2250 \\ 975 \\ 750 \end{gathered}$ | ns |
| ```Turn-On Delay Time Cin to S tPHL = (1.7 ns/pF) CL + 565 ns tPHL = (0.66 ns/pF) CL + 197 ns tPHL = (0.5 ns/pF) CL + 145 ns``` | tPHL | $\begin{aligned} & 5.0 \\ & 10 \\ & 15 \end{aligned}$ | - | $\begin{aligned} & 650 \\ & 230 \\ & 170 \end{aligned}$ | $\begin{aligned} & 1800 \\ & 600 \\ & 450 \end{aligned}$ | ns |

*The formulas given are for the typical characteristics only at $25^{\circ} \mathrm{C}$.
\#Data labelled "Typ" is not to be used for design purposes but is intended as an indication of the IC's potential performance.


Duty Cycle = 50\%
All outputs connected to respective $C_{L}$ loads
$\mathrm{f}=$ System clock frequency

Figure 1. Power Dissipation Waveforms


Figure 2. Switching Time Waveforms


One MC14560B and MC14561B permit a BCD digit to be added to or subtracted from a second digit, such as in this typical configuration. A second MC14561B permits either digit to be added to or subtracted from the other, or either word to appear unmodified at the output.

## TRUTH TABLE

| Zero | Add/Subtract | Result |
| :---: | :---: | :---: |
| 0 | 0 | B plus A |
| 0 | 1 | B minus A |
| 1 | $X$ | B |

$X=$ Don't Care


Figure 3. Parallel Add/Subtract Circuit

## APPLICATIONS INFORMATION

## INTRODUCTION

Frequently in small digital systems, simple decimal arithmetic is performed. Decimal data enters and leaves the system arithmetic unit in a binary coded decimal (BCD) format. The adder/subtracter in the arithmetic unit may be required to accept sign as well as magnitude, and generate sign, magnitude, and overflow. In the past, it has been cumbersome to build sign and magnitude adder/subtracters. Now, using Motorola's MSI CMOS functions, the MC14560 NBCD Adders and MC14561 9's Complementers, NBCD adder/ subtracters may be built economically, with surprisingly low package count and moderate speed.

Some background information on BCD arithmetic is presented here, followed by simple circuits for unsigned adder/ subtracters. The final circuit discussed is an adder/subtracter for signed numbers with complete overflow and sign correction logic.

## DECIMAL NUMBER REPRESENTATION

Because logic elements are binary or two-state devices, decimal digits are generally represented as a group of bits in a weighted format. There are many possible binary codes which can be used to represent a decimal number. One of the most popular codes using 4 binary digits to represent 0 thru 9 is Natural Binary Coded Decimal (NBCD or 8-4-2-1 code).

NBCD is a weighted code. If a value of " 0 " or " 1 " is assigned to each of the bit positions, where the rightmost position is $2^{0}$ and the leftmost is $2^{3}$, and the values are summed for a given code, the result is equal to the decimal digit represented by the code. Thus, 0110 equals $0 \cdot 2^{3}+1 \cdot 2^{2}+1 \cdot 2^{1}+$ $0 \cdot 2^{0}=4+2=6$. The 1010, 1011, 1100, 1101, 1110, and 1111 binary codes are not used. Because of these illegal states, the addition and subtraction of NBCD numbers is more complex than similar calculations on straight binary numbers.

## ADDITION OF UNSIGNED NBCD NUMBERS

When 2 NBCD digits, A and B, and a possible carry, C, are added, a total of 20 digit sums $(A+B+C)$ are possible as shown in Table 1.

The binary representations for the digit sums 10 thru 19 are offset by 6 , the number of unused binary states, and are not correct. An algorithm for obtaining the correct sum is shown in Figure 1. A conventional method of implementing the BCD addition algorithm is shown in Figure 2(a). The NBCD digits, $A$ and $B$, are summed by a 4 bit binary full adder. The resultant (sum and carry) is input to a binary/BCD code converter which generates the correct BCD code and carry.

An NBCD adder block which performs the above function is available in a single CMOS package (MC14560).

Figure 2(b) shows $n$ decades cascaded for addition of $n$ digit unsigned NBCD numbers. Add time is typically $0.1+0.2 n \mu s$ for $n$ decades. When the carry out of the most significant decade is a logical "1", an overflow is indicated.

## COMPLEMENT ARITHMETIC

Complement arithmetic is used in NBCD subtraction. That is, the "complement" of the subtrahend is added to the minuend. The complementing process amounts to biasing the subtrahend such that all possible sums are positive. Consider the subtraction of the NBCD numbers, A and B :

$$
R=A-B
$$

where $R$ is the result. Now bias both sides of the equation by $10 \mathrm{~N}-1$ where N is the number of digits in A and B .

$$
R+10 N-1 A-B+10 N-1
$$

Rearranging,

$$
R+10 N-1 A+(10 N-1-B)
$$

 the 9 's complement of $B$. When $A>B, R+10 N-1>10 N_{-1}$; thus $R$ is a positive number. To obtain $R, 1$ is added to $R+$ $10 \mathrm{~N}-1$, and the carry term, 10 N , is dropped. The addition of 1 is called End Around Carry (EAC).

When $A<B, R+10 N_{-1}<10 N_{-1}$, no EAC results and $R$ is a negative number biased by $10 \mathrm{~N}_{-1}$; thus $R+10 \mathrm{~N}_{-1}$ is the 9's complement of R.

## SUBTRACTION OF UNSIGNED NBCD NUMBERS

Nine's complement arithmetic requires an element to perform the complementing function. An NBCD 9's complementer may be implemented using a 4 bit binary adder and 4 inverters, or with combinatorial logic. The Motorola MC14561 9 's complementer is available in a single package. It has true and inverted complement disable, which allow straightthrough or complement modes of operation. A "zero" line forces the output to " 0 ". Figure 3 shows an NBCD subtracter block using the MC14560 and MC14561. Also shown are n cascaded blocks for subtraction of $n$ digit unsigned numbers. Subtract time is $0.6+0.4 \mathrm{n} \mu \mathrm{s}$ for n stages. Underflow (borrow) is indicated by a logical " 0 " on the carry output of the most significant digit. A " 0 " carry also indicates that the difference is a negative number in 9's complement form. If the result is input to a 9's complementer, as shown, and its mode controlled by the carry out of the most significant digit, the output of the complementer will be the correct negative magnitude. Note that the carry out of the most significant digit (MSD) is the input to carry in of the least significant digit (LSD). This End Around Carry is required because subtraction is done in 9's complement arithmetic.

By controlling the complement and overflow logic with an add/subtract line, both addition and subtraction are performed using the basic subtracter blocks (Figure 4).

Table 1. Sum $=A+B+C$

| Binary Sums | Decimal Numbers | Corrected Binary Sums |
| :---: | :---: | :---: |
| 0000 | 0 | 0000 |
| 0001 | 1 | 0001 |
| 0010 | 2 | 0010 |
| 0011 | 3 | 0011 |
| 0100 | 4 | 0100 |
| 0101 | 5 | 0101 |
| 0110 | 6 | 0110 |
| 0111 | 7 | 0111 |
| 1000 | 8 | 1000 |
| 1001 | 9 | 1001 |
| 1010 | 10 | 0000 + Carry |
| 1011 | 11 | 0001 + Carry |
| 1100 ( Non valid | 12 | 0010 + Carry |
| 1101 \} BCD | 13 | 0011 + Carry |
| 1110 representation | 14 | 0100 + Carry |
| 1111 | 15 | 0101 + Carry |
| 0000 + Carry | 16 | 0110 + Carry |
| 0001 + Carry | 17 | 0111 + Carry |
| 0010 + Carry | 18 | 1000 + Carry |
| 0011 + Carry | 19 | 1001 + Carry |

## ADDITION AND SUBTRACTION OF SIGNED NBCD NUMBERS

Using MC14560 NBCD Adders and MC14561 9's Complementers, a sign and magnitude adder/subtracter can be configured (Figure 5). Inputs $A$ and $B$ are signed positive (AS, BS $=$ " 0 ") or negative (As, BS = " 1 "). B is added to or subtracted from A under control of an Add/Sub line (subtraction = "1"). The result, $R$, of the operation is positive signed, positive signed with overflow, negative signed, or negative signed with overflow. Add/subtract time is typically $0.6+0.4 \mathrm{n} \mu \mathrm{s}$ for n decades.

An exclusive-OR of Add/Sub line and BS produces $B^{\prime}$, which controls the $B$ complementers. If $B_{S}$, the sign of $B$, is a logical " 1 " ( $B$ is negative) and the Add/Sub line is a " 0 " (add $B$ to $A$ ), then the output of the exclusive-OR ( $B_{S^{\prime}}$ ) is a logical " 1 " and $B$ is complemented. If $B=" 1$ " and $\operatorname{Add} / \mathrm{Sub}=" 1$ ", $B$ is not complemented since subtracting a negative number is the same as adding a positive number. When Add/Sub is a " 1 " and $B S=$ " 0 ", $B_{S}$ ' is a " 1 " and $B$ is complemented. The $A$ complementer is controlled by the A sign bit, As. When As = " 1 ", $A$ is complemented.


Figure 4. Unsigned NBCD Addition Algorithm

(a) MC14560 Block Diagram


Typical Add Time $=0.1+0.2 n \mu \mathrm{~s}$
where $\mathrm{n}=$ Number of Decades
(b) n-Decade Adder

Figure 5. Addition of Unsigned NBCD Numbers

The truth table and Karnaugh maps for sign, overflow, and End Around Carry are shown in Figures 6 and 7. Note the use of $\mathrm{Bs}^{\prime}$ from the exclusive-OR of Add/Sub and Bs. Bs' eliminates Add/Sub as a variable in the truth table. As an example of truth table generation, consider an n decade adder/ subtracter where $\mathrm{A} S=$ " 0 ", BS = " 1 ", and Add/Sub = " 0 ". B is in 9's complement form, $10 \mathrm{~N}_{-1}-\mathrm{B}$. Thus $\mathrm{A}+\left(10 \mathrm{~N}_{-1}-\mathrm{B}\right)$ $=10 \mathrm{~N}-1+(A-B)$. There is no carry when $A \leq B$, and the sign is negative (sign $=$ " 1 "). When AS and BS are opposite states and Add/Sub is a " 0 " (add mode), no overflow can occur (overflow = " 0 "). The other output states are determined in a similar manner (see Figure 6).

From the Karnaugh maps it is apparent that End Around Carry is composed of the two symmetrical functions S2 and S 3 of three variables with $\mathrm{As} \mathrm{BS}^{\prime} \mathrm{C}_{\text {out }}$ as the center of symmetry. This is the definition of the majority logic function $\mathrm{M}_{3}(\mathrm{ABC})$. Similarly the Sign is composed of the symmetrical functions S2(3) and S3(3) but with the center of symmetry
translated to $A_{S} B S^{\prime} C_{\text {out }}$. This is equivalent to the majority function $\mathrm{M}_{3}\left(\mathrm{~A}_{S} \mathrm{Bs}^{\prime} \overline{\mathrm{C}}_{\text {out }}\right)$. Further evaluation of the maps and truth table reveal that Overflow can be generated by the exclusive-OR function of End Around Carry and Carry Out. This analysis results in a minimum device count consisting of one exclusive-OR package and one dual Majority Logic package to implement $\mathrm{BS}^{\prime}$, EAC, Sign and Overflow. The logic connections of these devices are shown in Figure 5.

The output sign, R $\mathrm{R}_{\mathrm{S}}$, complements the result of the add/ subtract operation when $\mathrm{R}_{\mathrm{S}}=$ " 1 ". This is required because the adder performs 9's complement arithmetic. Complementing, when RS indicates the result is negative, restores sign and magnitude convention.

Several variations of the adder/subtracter are possible. For example, 9's complement is available at the output of the NBCD adders, and output complementers are eliminated if sign and magnitude output is not required.


Figure 6. Subtraction of Unsigned NBCD Numbers

## SUMMARY

The concepts of binary code representations for decimal numbers, addition, and complement subtraction were discussed in detail. Using the basic Adder and Complementer MSI blocks, adder/subtracters for both signed and unsigned numbers were illustrated with examples.

## REFERENCES

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2. McMOS Handbook, Motorola Inc., 1st Edition.
3. Beuscher, H.: Electronic Switching Theory and Circuits, New York, Van Nostrand Reinhold, 1971.
4. Garrett, L.: CMOS May Help Majority Logic Win Designer's Vote, Electronics, July 19, 1973.
5. Richards, R.: Digital Design, New York, WileyInterscience, 1971.


Typical Add/Subtract Time $=0.6+0.4 \mathrm{n} \mu \mathrm{s}$ where $\mathrm{n}=$ Number of Decades

Figure 7. Adder/Subtracter for Unsigned NBCD Numbers


Figure 8. Sign and Magnitude Adder/Subtracter with Overflow

| Inputs |  |  | Arithmatic Expression for R* (Result) ( $\mathrm{N}=$ Number of Digits, $10^{\mathrm{N}}=$ Modulus $\mathrm{A}, \mathrm{B}, \mathrm{R}$ are Positive Magnitudes) | Outputs |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { AS } \\ " 1 "=\text { Neg } \end{gathered}$ | $\begin{gathered} \mathrm{BS}^{\prime} \\ " 1 "=\mathrm{Neg} \end{gathered}$ | $\begin{gathered} \text { Cout } \\ " 1 "=\text { Carry } \end{gathered}$ |  | End Around Carry (EAC) "1" = EAC | Sign of $R$ "1" = Negative | Overflow "1" = Overflow |
| 0 | 0 | 0 | $\mathrm{R}=\mathrm{A}+8$ | No EAC ("0") because R is correct result. | Since $A$ and $B$ are positive signed, $R$ is positive signed ("0"). | When $\mathrm{C}_{\text {out }}=$ " 0 ", there is no carry ( $\mathrm{R}<10 \mathrm{~N}$ ) and thus no overflow ("0"). |
| 0 | 0 | 1 |  |  |  | When $\mathrm{C}_{\text {out }}=$ " 1 ", there is a carry $(R \geq 10 \mathrm{~N})$ and thus overflow ("1"). |
| 0 | 1 | 0 | $\begin{aligned} R & =A-B \\ & =A+\left(10 N_{-1}-B\right) \\ & =A-B+10 N_{-1} \end{aligned}$ | No EAC ("0") because 9's complement expression for $R$ is correct result. | $\mathrm{A} \leq \mathrm{B}$ when $\mathrm{C}_{\text {out }}=$ " 0 "; thus sign of $R$ must be negative ("1"). |  |
| 0 | 1 | 1 |  | $\mathrm{EAC}=$ " 1 " because expression for $R$ is in error by 1 . | $\mathrm{A}>\mathrm{B}$ when $\mathrm{C}_{\text {out }}=$ "1"; thus sign of R must be positive ("0"). | There is never an overflow when |
| 1 | 0 | 0 | $\begin{aligned} R & =B-A \\ & =B+(10 N-1-A) \\ & =B-A+10 N-1 \end{aligned}$ | No EAC ("0") because 9's complement expression for R is correct result. | $\mathrm{B} \leq \mathrm{A}$ when $\mathrm{C}_{\text {out }}=$ " 0 "; thus sign of $R$ must be negative ("1"). | numbers of opposite sign are added. |
| 1 | 0 | 1 |  | EAC = " 1 " because expression for $R$ is in error by 1 . | B > A when $\mathrm{C}_{\text {out }}=$ "1"; thus sign of R must be positive ("0"). |  |
| 1 | 1 | 0 | $\begin{aligned} R & =-A-B \\ & =(10 N-1-A)+ \\ & (10 N-1-B) \\ & =-(A+B)+2 x \end{aligned}$ | EAC = " 1 " because 9's complement expression for $R$ is in error by 1 . | Since $A$ and $B$ are negative signed. $R$ is negative signed ("1"). | When $\mathrm{C}_{\text {out }}=$ " 0 ", there is no Carry $(R<0 N)$ and $(A+B)>10 \mathrm{~N}_{-1}$ indicating overflow ("1"). |
| 1 | 1 | 1 |  |  |  | When $\mathrm{C}_{\text {out }}=$ " 1 ", there is a carry $(R \geq 10 \mathrm{~N})$ and $(\mathrm{A}+\mathrm{B}) \leq 10 \mathrm{~N}-1$ indicating no overflow ("0"). |

[^0]Figure 9. Truth Table Generation for EAC, Sign, and Overflow Logic

TRUTH TABLE

| Inputs |  |  |  | Outputs |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{A S}_{\mathbf{S}}$ | B $^{\prime}$ | C $_{\text {out }}$ | EAC | SGN | OVF |  |
| 0 | 0 | 0 | 0 | 0 | 0 |  |
| 0 | 1 | 0 | 0 | 1 | 0 |  |
| 1 | 0 | 0 | 0 | 1 | 0 |  |
| 1 | 1 | 0 | 1 | 1 | 1 |  |
| 0 | 0 | 1 | 0 | 0 | 1 |  |
| 0 | 1 | 1 | 1 | 0 | 0 |  |
| 1 | 0 | 1 | 1 | 0 | 0 |  |
| 1 | 1 | 1 | 1 | 1 | 0 |  |

$\mathrm{B}_{\mathrm{S}}=(\mathrm{Add} / \mathrm{Sub}) \oplus \mathrm{BS}_{\mathrm{S}}$
$\mathrm{A}_{\mathrm{S}}=$ Sign of A ("1" = Negative)
BS = Sign of B ("1" = Negative)
Cout $=$ Adder Carry Out

KARNAUGH MAPS


* $=$ Center of Symmetry

$$
\begin{aligned}
E A C & =S 2\left(A_{S} B_{S}{ }^{\prime} C_{o u t}\right)+S 3\left(A_{S} B_{S^{\prime}} C_{o u t}\right) \\
& =M_{3}\left(A_{S} B^{\prime} S^{\prime} C_{o u t}\right) \\
S G N & =S 2\left(A_{S} B^{\prime} \bar{C}_{\text {out }}\right)+S 3\left(A_{S} B S^{\prime} C_{\text {out }}\right) \\
& =M_{3}\left(A_{S} B^{\prime} S^{\prime} C_{o u t}\right)
\end{aligned}
$$

$c \mid$ EAC

| 0 | 1 |
| :--- | :--- |
| 1 | 1 |
| 0 | 1 |
| 0 | 0 |$\oplus$| 0 | 0 |
| :---: | :---: |
| 1 | 1 |
| 1 | 1 |
| 0 | 0 |$\quad=$| 0 | 1 |
| :---: | :---: |
| 0 | 0 |
| 1 | 0 |
| 0 | 0 |

Figure 10. Mapping of EAC, Sign and Overflow Logic


## D SUFFIX

PLASTIC SOIC PACKAGE
CASE 751B-05
ISSUE J


NOTES:

1. DIMENSIONING AND TOLERANCING PER ANSI Y14.5M, 1982.
2. CONTROLLING DIMENSION: MILLIMETER.
3. DIMENSIONS A AND B DO NOT INCLUDE MOLD PROTRUSION.
4. MAXIMUM MOLD PROTRUSION $0.15(0.006)$ PER SIDE.
5. DIMENSION D DOES NOT INCLUDE DAMBAR PROTRUSION. ALLOWABLE DAMBAR PROTRUSION. ALLOWABLE DAMBAR
PROTRUSION SHALL BE $0.127(0.005)$ TOTAL PROTRUSION SHALL BE 0.127 ( 0.005 )
IN EXCESS OF THE D DIMENSION AT IN EXCESS OF THE D DIMENSION A
MAXIMUM MATERIAL CONDITION.

| DIM | MILLIMETERS |  | INCHES |  |  |
| :---: | ---: | ---: | ---: | ---: | :---: |
|  | MIN |  | MAX | MIN |  |
| MAX |  |  |  |  |  |
| A | 9.80 | 10.00 | 0.386 | 0.393 |  |
| B | 3.80 | 4.00 | 0.150 | 0.157 |  |
| C | 1.35 | 1.75 | 0.054 | 0.068 |  |
| D | 0.35 | 0.49 | 0.014 | 0.019 |  |
| F | 0.40 | 1.25 | 0.016 | 0.049 |  |
| G | 1.27 |  | BSC | 0.050 BSC |  |
| J | 0.19 | 0.25 | 0.008 | 0.009 |  |
| K | 0.10 | 0.25 | 0.004 | 0.009 |  |
| M | 0 | $7^{\circ}$ | $7^{\circ}$ | $0^{\circ}$ |  |
| P | 5.80 | 6.20 | 0.229 | $7^{\circ} 0.244$ |  |
| R | 0.25 | 0.50 | 0.010 | 0.019 |  |

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[^0]:    * Output of Adders

